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GENERAL MACROECONOMIC CLOSURE IN  
APPLIED GENERAL EQUILIBRIUM MODELLING:  
Experience from ORANI and  
Agenda for Further Research  
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## NOTES

- \* Aspects of the long-run macroeconomic closure of ORANI are discussed by Dixon, Parmenter and Rimmer (1984), by Powell, Cooper and McLaren (1983), Section 3, and by Horridge and Powell (1984).
1. In his later work, Walras himself took the initial steps in extending his framework to include a monetary asset. For a critique of this attempt, see Patinkin (1965), pp.541-572. An important initial step in the extension of the Walrasian paradigm in applied work was the 'helicopter drop' assumption made by Clements (1980) who treated domestic credit expansion as an exogenous variable, but one entailing real monetary effects in the short run. Kehoe (1981) also adds government debt (but not money) to the Walrasian real system. Another group of authors (e.g., Piggott (1981)) explore the real effects which an exogenous inflation produces via the failure, in varying degrees, of the different elements of the tax system to be fully and instantaneously indexed to the general price level.
  2. In this section we draw freely on Cooper and McLaren (1980), (1982), (1983), and on Cooper (1983).
  3. The table of elasticities - the derivatives of elements of  $Y_0$  with respect to elements of  $Z_0$  (the matrix  $C_0$ ) - is given in Appendix 2 of Powell, Cooper and McLaren (1983). The numerical values of these elasticities correspond to the underlying numerical data base and parameter values of ORANI8 used in the tariff experiment reported in DPSV (1982), Chapter 7. The split of variables into endogenous and exogenous sets corresponds to the standard short-run neoclassical model with a slack labour market. The table of elasticities is therefore a subset of a standard basic solution of ORANI8. It may be noted that the numeraire of the model is the exchange rate and, with respect to this variable, the model is homogenous of degree zero in reals and one in nominal.
  4. MACRO endogenizes the number of persons employed, whereas ORANI endogenizes total labour hours. This led to the addition to the system of the equation
- $$d \log L_h = d \log L + n (d \log Y - d \log Y^*)$$
- where  $L_h$  is labour hours,  $L$  is persons employed,  $Y$  is output and  $Y^*$  is the output level corresponding to "standard hours".  $n$  was treated as an interface parameter; its estimated value, 0.45, was determined jointly with the seven other interface parameter estimates reported in Table 3. For further details, see Cooper (1983), pp.8-9.

## SHORT-RUN\* MACROECONOMIC CLOSURE IN APPLIED

## GENERAL EQUILIBRIUM MODELLING :

Experience from ORANI and Agenda for Further Research

by

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### 1. INTRODUCTION

Perhaps most important among the contentious issues remaining in applied general equilibrium modelling is the role (if any) of conventional macroeconomics. Models in the Walrasian tradition are comparative static in nature; they are not well suited, therefore, to the analysis of transitory phenomena such as the stage of the business cycle. When our policy-analytic models are focussed at one or two years into the hypothetical future, however, it may be impossible to ignore transients and remain convincing. In other words, we may be required to tell a story which is part Walrasian and part macroeconomic. How can such an unlikely hybrid be seeded?

#### 1.1 The extended Walrasian paradigm

Several approaches are possible. The cleanest, of course, involves a Walrasian take-over bid for macroeconomics. In such an extended Walrasian paradigm demand and supply functions for money and perhaps other financial assets are added to the real system (Patinkin (1958); Feltensteiner (1981); Vincent (1983)!). This introduces at least one additional agent (the supplier of money, usually the government), and the opportunity to endogenize such important macroeconomic variables as the price level and the money supply.

In terms of applied work, it is early days yet for the extended Walrasian paradigm. If eventually it turns out that transients with expected lives of (say) less than a year cannot really be modelled successfully using the tools of economic analysis, then the limitations inherent in the comparative static nature of the extended Walrasian method may come to be accepted as the state of the art for the analysis

of short-run issues. In the meantime there is a large profession engaged in applied macrodynamic analysis who claim otherwise. Taking their claim (provisionally) at its face value, is there a method of incorporating macrodynamic insights within a Walrasian framework?

### 1.2 The IMPACT paradigm

The institutional environment within which the IMPACT project was set up provided a strong incentive to find an affirmative answer to the preceding question. While necessarily we were required to concentrate on the real economy and relative prices because of our principal backer's (the Industries Assistance Commission, IAC's) interest in international trade and industry protection, and while also we were required to build a model which would produce sectoral policy recommendations in harmony with the thrust of the government's macroeconomic policy, under no circumstances were we to build our own macro models. The latter interdiction was motivated by two considerations: one survival oriented, the second more honourable. The former could be paraphrased as "Keep off the Treasury's turf, or you know what!", while the latter simply recognized that the community had already made a very large investment in macrodynamic analysis, especially at the Reserve Bank and at the Treasury. Macroeconomic insights, if such were available, were to be harvested from the work of others. In due course these motivations led to the development of the IMPACT Paradigm. The latter allows a macrodynamic model to determine all of the major monetary, financial and macroeconomic aggregates simultaneously with the determination by a computable general equilibrium (CGE) model of relative prices and the commodity and factor composition of the economy along strictly Walrasian lines.

## 2. MACROECONOMIC CLOSURE OF A CGE: BASIC CONCEPTS

### 2.1 Basic closure

The term 'closure' is used in various ways, and with varying degrees of precision, in our literature. At the most basic level we say that a model is 'closed' if we have sufficient information to compute a solution. It will suffice here to restrict attention to linear models. Let  $M_t$

$$M_t : Ax = 0 \quad (1.1)$$

Monetary and other transient phenomena are involved in short-run economic analysis. Essentially two options are available for the short-run macro-closure of ORANI: (i) the extended Walrasian paradigm and (ii) the IMPACT paradigm. (A third option, currently on the back-burner because of the probably insurmountable data problems inherent in the estimation of its additional parameters, endows every ORANI micro-variable with its own adjustment path - see FitzGerald (1979).) During the last four years work at IMPACT has concentrated on (ii). This work has resulted in an operational method for interfacing a small macrodynamic model in the Bergstrom-Wymer (1976) class with a large CGE model in the Johansen (1960) class (Cooper and McLaren (1980), (1982), (1983); Cooper (1983)). It is hoped that other researchers will extend the range of simulations made with the interfaced system; above we have reported only the (aggregate) results for a shock in government spending (used to calibrate the interface) and for a uniform tariff change. In 1984 we have initiated work on the extended Walrasian paradigm with a view to comparative analysis of its performance against that of the IMPACT paradigm.

TABLE 4  
PRINCIPAL RESULTS OF A 25 PER CENT TARIFF INCREASE IN THE ORANI-MACRO SYSTEM\*

Endogenous Variable	ORANI Response within the Intefaced System		MACRO Response within the Intefaced System	
	(I)	(II)	(III)	(IV)
$y_g$	Output	-0.089	-0.123	-0.089
$p$	Prices	1.862	1.805	-0.374
$I_h$	Employment	-0.167	-0.205	-0.082
$i$	Imports $(x P_x)$	-1.322	-1.528	-3.625
$E$	Value of Exports (\$us)	-2.824	-2.523	n.a.
w/p	Exchange Rate (\$N/\$us)	n.a.	n.a.	-0.237
k	Real Wages	n.a.	n.a.	0.104
	Rate of Net Investment	n.a.	n.a.	0.003
K	Capital Stock	n.a.	n.a.	0.112
d	Household Expenditure	n.a.	n.a.	-0.053

\* Based on the interface parameters shown in Table 3 and  $t_3 = 0.15923$ . For further details, see Cooper (1983). Figures in the table are percentage deviations from control at 7.94 quarters after the tariff shock.

n.a. not applicable

(a) a declaration that a certain subset  $x_2$  of  $x$  containing  $(k-m)$  variables is exogenous  
(b) an assignment of a set of values (say  $\bar{x}_2$ ) to these exogenous variables.

Sometimes the term 'closure' is used loosely to describe (a) alone. In that case, closure means that we could, if we were to make an assignment (b), solve the model. Since the variables  $x_2$  are exogenous, their assignment can be completely arbitrary, and hence these two primitive notions of closure boil down to the same thing.

#### 2.2 Closure with respect to a subset of variables

A second notion of closure is defined relative to some subset of the model's variables. We say that  $M$  is closed with respect to the variables  $x^m$  ( $x^m \subset x$ ) provided the variables  $x^m$  are endogenized by the model in the context of the basic closure selected. Thus  $M$  is closed with respect to  $x^m$  if the  $x_2$  chosen in (a) is such that  $x^m$  and  $x_2$  have no elements in common. 'Macroeconomic closure' is of this second type. In this case the components of  $x^m$  will include the real values of major aggregates (consumption, investment) plus a range of monetary and financial variables (the exact list will depend upon the application). Macroeconomic closure is then achieved by ensuring that  $M$  has sufficient equations to endogenize these variables in the context of a suitable partition of the variables  $x$  into the endogenous and exogenous categories. Here 'suitable' has two implications:

- (i) in partitioning  $x$  into  $[x_1, x_2]$  (where  $x^m \subset x_1$ ) so that becomes

$$Ax = 0$$

the choice made must result in  $A_1$  having full rank;  
and

Source: Cooper (1983).

(ii) no variable (outside the set  $x^m$ ) which the model is required to explain may be assigned to the exogenous set  $x_2$ . Condition (i) is required in order to obtain a unique solution of  $M(x_1 = -A_1^{-1} A_2 x_2)$ , while condition (ii) ensures that macroeconomic closure is not obtained at the expense of other purposes for which the model was built.

### 2.3 Short versus long-run closure

The first crucial difference between short and long-run modelling is in the choice of variables to be included in the model. While transients may play important roles in short-run modelling, by definition they have no place in the long run. If transient variables are included in a model to be used in a long-run closure, they should appear on the exogenous list where they should be assigned neutral values. Alternatively, it should be a property of the model's structure that such transient variables can be guaranteed endogenously to take on neutral values in a long solution. If the focus is on the long run, then in keeping with the long-run neutrality of money, variables included in  $x^m$  (and therefore within  $x_1$  in a macroeconomically closed model) should be real stocks or flows, or relative prices.

In the standard version of IMPACT's CGE model, ORANI (Dixon, Parmenter, Sutton and Vincent (1982) - hereafter DPSV (1982)) provision is made for the user to select his own basic closure (DPSV (1982), Ch.7). The choice of endogenous and exogenous sets  $x_1$  and  $x_2$  (along with some choices about the values of behavioural parameters) crucially affects the interpretation of the comparative static time frame. In ORANI's standard (or neo-classical) short-run closure, the elapsed time between the base-period and the attainment of the new solution is assumed to be sufficiently short to allow one to ignore the impact of the shock under analysis on capital stocks in use in each industry, but sufficiently long for relative prices, consumption, investment demands and production of every commodity to have reached a new equilibrium configuration. (As will be seen below, such a short-run concept might well correspond in calendar time to about two years.) With capital stocks fixed, rates of return in the different industries are endogenous. If we reverse the roles of these two sets of variables - i.e., we take industry rates of return as exogenous and endogenize the

The principal results of the tariff experiment are given in Table 4. The main feature to note is the strong similarity between columns I and II, and the extent of the divergence between them and column III.

Column II shows the 'macroeconomically compensated' values of the responses of the major macroeconomic aggregates to a 25 per cent increase in tariffs. This is the standard ORANI, stand-alone, story. Column I shows how the ORANI story must be modified to allow for the impact of the tariff shock on the macroeconomic environment. These results in column I are based on the interface parameters shown in Table 3. The overwhelming impression gained by comparison of columns I and II is that the change in the macroeconomic environment induced by the tariff shock has only second order consequences to major macroeconomic aggregates.

Comparison of columns I and III of Table 4 reveals that MACRO and ORANI want to tell somewhat different stories about the impact of the tariff rise. By construction, their output responses were made identical (-0.089%) by selection of a suitable value of  $t_3$  (the average tariff level). It will be noted that the MACRO responses in employment and output are equal, whereas ORANI shows the standard neo-classical short run result in which the employment response is a multiple (namely, 1.9) of the output response. Imports decline according to both sides of the interfaced model; the MACRO response, however, is 2 to 3 times larger in absolute value. The key to this is the behaviour of the price level in MACRO, which is the glaring inconsistency. It seems here difficult to accept the MACRO result that a 25 per cent increase in tariffs could be deflationary at a two year lag. Given this result, however, the consequent increase in the competitiveness of the domestic economy leads in MACRO to a substantial decline in imports. It may be expected that, in the presence of an experiment involving a highly non-neutral shock, the model which has been built more specifically for analysis of the type of shock in question would give the more reasonable results. In the above case it is not surprising that the ORANI results for a tariff shock would be the more reasonable.

### 9. CONCLUSION AND PROSPECT FOR FURTHER RESEARCH

The ORANI model is an example of a large CGE model used routinely for policy analysis. It is not macroeconomically closed.

TABLE 3  
ESTIMATED VALUES OF MAIN INTERFACE PARAMETERS

ORANI Variables	Adjustment Speeds (Diagonal elements of $\mathbf{A}_0$ )	Solution Values at $t^*$ of the Double Endogeneities** (I)	
		Double Endogeneities** (II)	
$y_g$	Output	$\beta_1 = 4.39$	1.073
$P$	Domestic Prices	$\beta_2 = 74.4$	1.358
$L_h$	Employment	$\beta_3 = 9.8$	1.557
$i$	Imports	$\beta_4 = 5.9$	1.854
$P_{wl}$	Price of Wool	$\beta_5 = 10$	n.a.
$x, P_x, (x, P_x)$	Export Sector	$\beta_6 = .5$	n.a.

ORANI Response Interval :  $t^* = 7.94$  quarters

\*\* Result shown in column II applies to both the ORANI and MACRO projections of the doubly endogenous variable within the interfaced ORANI-MACRO system. At the given parameter settings, the two projections are in fact identical to the fourth decimal place. Further details are available in Appendix 3 of Powell, Cooper and McLaren (1983), where a comparison is given with solution values for  $t^*$  set at 7.93 and 7.95 quarters.

n.a. Not applicable (variable is not doubly endogenous).

vector of capital stocks - then, clearly, a longer time-frame must be involved. In fact this is what is done in long-run closures of ORANI, where it is assumed that, relative to the world capital market, Australia is a small country. Given that any initial deviations in Australian industries' relative and absolute rates of return from the competitive world-wide values of these variables are eliminated, in the long run, by accumulation or decumulation of capital, what are the sources of such capital?

#### 2.4 ORANI's lack of long-run macroeconomic closure

It is at this point that ORANI's lack of long-run macroeconomic closure becomes evident: The standard version of ORANI focusses heavily on commodity markets, and on the demand side of the labour market, but does not deal with financial or capital markets. To provide long-run macroeconomic closure it is necessary to add additional equations in order to endogenize the real flow of foreign capital. Inter alia this involves also endogenizing real saving and consumption (not usually endogenous in closures of the standard version of ORANI). The basic approach for such an extension of ORANI has been developed by Dixon, Parmenter and Rimmer (1984).

#### 2.5 ORANI's lack of short-run macroeconomic closure

In a standard short-run closure of the standard version of ORANI, the following variables of macroeconomic interest are routinely assigned to the exogenous set  $x_2$ :

- (i) one of the price level or the exchange rate (as numeraire),
- (ii) one of the real wage or the aggregate level of employment,
- (iii) one of real absorption ( $C+I+G$ ) or the balance of trade surplus ( $X-M$ ).

These three choices are forced on users of ORANI (in stand-alone mode) because there are no mechanisms in the model suitable for determining

- (i) the extent to which induced changes in the real exchange rate will be realized as changes in the domestic inflation rate relative to the foreign rate or as changes in the nominal exchange rate;

Source: Cooper (1983).

- (II) the extent to which induced changes in the buoyancy of the labour market will be realized as changes in real wages or as changes in employment;
- (III) the extent to which induced changes in national income will be realized as changes in aggregate absorption or as changes in the balance of trade.

Thus at the outset three important macro variables must be exogenized in stand-alone applications of ORANI. But there are further macro variables, such as interest rates, the money stock, the stock of bonds held by the non-bank sector and the level of foreign reserves, which do not appear in ORANI at all. If these are to be included in  $x^m$ , then additional equations are needed for short-run macroeconomic closure.

### 3. THE IMPACT APPROACH TO SHORT-RUN MACROECONOMIC CLOSURE<sup>2</sup>

The IMPACT paradigm is based on the following, strong, maintained hypothesis: in the short run

"... financial and money markets, as well as fiscal actions, are only important for individual industries insofar as they exert a real effect on the big components of national income: namely, private consumption, private capital formation, and government spending" (Powell (1981), p.242).

Under this paradigm the absence of monetary and financial variables in ORANI is no embarrassment since the economy is visualized as being separable between its macro (including financial and monetary) components on the one hand, and its micro (especially sectoral, and relative price) components on the other. Indeed there are some virtues in carrying out simulations with ORANI in an exogenous macroeconomic environment: there are, after all, a set of macro instruments available to sterilize any unwanted macro consequences of sectoral and relative price shocks.

Nevertheless we have found that policy advisers are preoccupied with these macro consequences (probably because their potential sizes have been seriously overestimated, especially in the case of tariff-related shocks). Thus the problem has required serious attention.

3.1 The nature of an ORANI solution

The comparative static method can be used in two essentially different ways. In the first, two equilibria which are supposed to occur

would be expected to be working themselves out. A priori this interval was expected to be in the range 6 to 8 quarters and an intensive search over 5 to 12 quarters was carried out.

The criterion for choice of the interface parameters was the minimization of the (unweighted) sum of squared deviations of the double endogeneities when evaluated at  $t^*$ . An intensive search over an eight-dimensional space<sup>4</sup> led to the parameter values shown in column I of Table 3.

Besides the estimates of the main interface parameters, this table also shows the values, at these parameter settings, of the doubly endogenous variables. These figures correspond to a shock of 10.0 to log  $g_1$ , government expenditure, and may be interpreted as percentage responses to a 10 per cent shock. The method has been successful in finding a setting for the interface parameters which eliminates inconsistency between ORANI and MACRO under a shock in government spending.

### 8. RESULTS FOR A TARIFF SHOCK

Using the above parameter values, this experiment shocked  $t_3$ , the average tariff variable in ORANI, by 25 per cent. A search over  $t_3$  to determine the appropriate corresponding shock to  $(1 + t_3)$ , the power of the tariff variable in MACRO, subject to the criterion of minimizing the squared difference between the ORANI and MACRO projections of the output double endogeneity, led to the following results:

Shock to $(1 + t_3)$ :	3.434%
Implied value of $t_3$ :	15.923%
Value of real output ( $y_g$ ) as computed by both the MACRO and ORANI components of the interfaced system :	-0.089%

This implied value of  $t_3$  (approximately 16 per cent) is of broadly comparable size to more direct estimates by the Industries Assistance Commission (1980, Table 2.1). Using weights based on the unassisted value of domestic production of commodities, the average tariff levels on manufactured products were estimated by the Commission to be 24 per cent in 1968-69, and 15 per cent in 1977-78.

The standard simulation consisted of a 10 per cent increase in real government spending. Other than the average tariff rate, this is the only double exogeneity. The main interface parameters to be estimated are:

- (i) the speeds of adjustment (i.e., the elements of the matrix  $A_0$ ). For parsimony of parameterisation this matrix is chosen to be diagonal. This has the advantage of assigning at most one adjustment speed parameter to each ORANI equation. Since usually only the aggregate versions of ORANI equations are used explicitly in the interfaced system, this provides a simple identification of an adjustment speed which may subsequently be applied to some subset of the general ORANI disaggregated families of equations. For the model specification given above the matrix  $A_0$  is of dimension 8 and the respective adjustment speeds relate to the following variables:

<u>ORANI Variable</u>	<u>Adjustment Speed</u>
1. $Y_g$ Real Gross Domestic Product	$\beta_1$
2. $P$ Price Deflator for Aggregate Production	$\beta_2$
3. $I_h$ Aggregate Employment Demand (labour-hours)	$\beta_3$
4. $i$ Real imports	$\beta_4$
5. $P_{wl}$ Price of Wool	$\beta_5$
6. $x$ Real Exports	$\beta_6$
7. $P_x$ Price of Exports (\$US)	$\beta_6$
8. $x_{P_x}$ Foreign currency value of Exports	$\beta_6$

Since variable 8 must be assigned an adjustment speed which is consistent with variables 6 and 7, these are constrained to a common adjustment speed ( $\beta_6$ ). The remaining five adjustment speeds are freely chosen. The parameterisation is in fact made upon  $\epsilon^{A_0}$ , so that the field of search is the six-dimensional positive orthant.

- (ii) the ORANI "short run",  $t^*$ : the length of time during which the effects calculated from an ORANI stand-alone experiment

at different points in time are compared. In the second, the differentials between two equilibria occurring at the same national period of time are calculated. The difference between the values  $y_A$  and  $y_B$  of a given endogenous variable  $y$  at a given point of time in two equilibrium solutions is then attributed to differing scenarios A and B which vary with respect to the settings of the exogenous variables. Thus the computed value ( $y_A - y_B$ ) answers the question:

By how much would  $y$  differ at time  $\tau$  as the result of making the assumptions A about the exogenous variables rather than the assumptions B?

Here the assumptions B define ceteris paribus and generate the control values  $y_B$  of the endogenous variables. In ORANI simulations this second method (contemporaneous differential comparative statics – cdcs for short) will almost always be the relevant approach. While all pretence of forecasting is eschewed in cdcs, the policy questions addressed come into sharper focus.

### 3.2 Problems of the interface

Our approach is to use a small macrodynamic model, MACRO, to close ORANI in short-run simulations. MACRO is a slightly revised mid 1979 version of the Reserve Bank of Australia's RBII model (Jensen and Trevor (1981) – see also Cooper (1983), p.28). This attempt to interface a comparative static model with a macrodynamic model threw up some substantial theoretical challenges. Among the more notable ones are:

- (i) the lack of an explicit dynamics in ORANI,
- (ii) temporal aggregation problems,
- (iii) the presence of variables which are endogenous to both models,
- (iv) differing definitions in the two models of essentially the same variables,
- (v) the presence in MACRO of macrorelations which cannot be derived as explicit aggregates of microrelations in ORANI (e.g., the production function),
- (vi) the difficulty of preserving homogeneity properties in the interfaced system.

The interfacing method developed by Cooper and McLaren (1980, 1982, 1983) seems to resolve the first four of these simultaneously. The

difficulties posed by (v) and (vi) seem to be irreducible liabilities of the method. In particular one cannot expect a separately developed macro model to be formulated in terms of perfect aggregates (where such exist) of the variables appearing in a given CGE model, nor could one expect the interfaced system to display excess supply functions for commodities which are homogeneous of first degree in the monetary stock and in nominal prices (see Weintrab (1974), p.51). On these two points of theoretical consistency the extended Walrasian paradigm offers better prospects.

Some of these problems were minimized by the particular macro model chosen. MACRO is a Bergstrom-Wymer model formulated in continuous time (see Bergstrom and Wymer (1976)). This continuous time formulation made solution of the temporal aggregation problem much easier. The relatively extensive coverage of money and financial markets, both of which are totally lacking in ORANI, was an advantage, as was the small size of MACRO (26 equations) and the consequent relatively infrequent occurrence of double endogeneities. Indeed, as we will see below, the double endogeneities were actually turned to advantage in the development of the interfacing methodology. This was possible because these variables provide a link between ORANI solutions and realizations of observable variables in real time.

### 3.3 Basic approach

The cdcs interpretation of ORANI solutions gels nicely with the macrodynamic method: in both cases attention is focussed on deviations from control. In the case of MACRO, such deviations can be computed for all instants of continuous time after the injection of a shock. A short-run solution of ORANI, on the other hand, only projects a single deviation from control at a single point of time after this shock. The interfacing methodology is based on attempting to identify an instant after an exogenous shock which reconciles these two stories. The elapsed time then provides an estimate of the ORANI short run  $t^*$ .

For the moment take it as given that some method of supplying feedbacks to ORANI from MACRO can be found. (With only a minor oversimplification, for the moment we ignore feedbacks from ORANI to MACRO.) Call the resulting system ORANI-MACRO (O-M). The response of this system will be shown below to be a function of the unknown length  $t^*$  of the ORANI short run (and of certain other parameters). The response

TABLE 2  
A PARTIAL LISTING OF VARIABLES APPEARING IN MACROB1

	Variables Endogenous to MACROB1 (A Subset of $Y_M$ )		Variables Exogenous to MACROB1 (A Subset of $Z_M$ )	
1.	$\log Y_g$	Real Gross Domestic Product	1.	$\log P_W$
2.	$\log P$	Price Deflator for Aggregate Production (\$A)	2.	$\log g_1$
3.	$\log I_h$	Aggregate Employment Demand (labour-hours)	3.	$\log (1+t_3)$
4.	$\log i$	Real Imports	4.	$\log P_{W1}$
5.	$\log E$	Exchange Rate (\$A/\$US)	5.	$\log g_1$
6.	$\log W$	Nominal Wages (average weekly earnings, \$A)	6.	$\log (1+t_3)$
7.	$\log d$	Aggregate Real Household Expenditure (including investment in dwellings)	7.	$\log P_i$
8.	$\kappa$	Proportional Change in New Investment (=DK/K)	8.	$\log P_W$
9.	$\log K$	Business Fixed Capital Stock	9.	World Prices (\$US)
		Variables Exogenous to MACROB1 (A Subset of $Z_M$ )		
1.		Price of Wool (\$US)	1.	
2.		Real Exports	2.	
3.		Price of Exports (\$A)	3.	
4.		Government Expenditure	4.	
5.		Power of Tariff	5.	
6.		Price of Imports (\$US)	6.	
7.		World Prices (\$US)	7.	

Source: Cooper (1983)

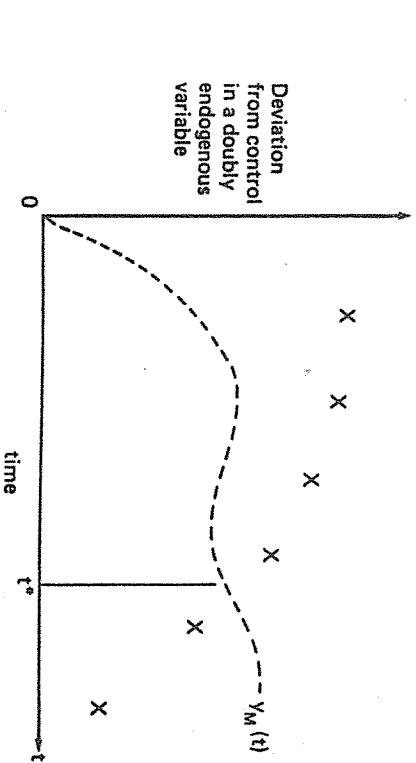
TABLE 1  
A PARTIAL LISTING OF VARIABLES APPEARING IN ORANI<sup>17</sup>

Variables Endogenous to ORANI: The Vector $y_0$	
1.	log $Y_g$ Real Gross Domestic Product
2.	log $P$ Price Deflator for Aggregate Production (\$A)
3.	log $I_h$ Aggregate Employment Demand (labour-hours)
4.	log $i$ Real Imports
5.	log $P_{WL}$ Price of Wool (\$A)
6.	log $x$ Real Exports
7.	log $P_x$ Price of Exports (\$US)
8.	log $(x P_x)$ Foreign Currency Value of Exports (\$US)

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Variables Exogenous to ORANI: The Vector $z_0$	
1.	log $E$ Exchange Rate (\$A/\$US)
2.	log $(W/P)$ Real Wages
3.	log $C_R$ Real Household Expenditure
4.	log $I_R$ Real Private Investment
5.	log $K(0)$ Initial Capital Stocks
6.	log $g_1$ Government Expenditure
7.	log $t_3$ Average Level of Tariffs

Figure 1. A shock is injected at  $t=0$ . The deviation-from-control in a doubly endogenous variable  $Y, Y_M(t)$ , as endogenized as a function of real time by MACRO, is shown as the broken line - - -. Within ORANI-MACRO, the ORANI contemporaneous differential comparative static solutions for the same variable at  $t$  (where  $t$  is the assumed length of the ORANI short run), are shown as  $x x x$ . At  $t^*$  the MACRO and ORANI stories are reconciled.



Source: Cooper (1983)

simultaneously provides an indirect real time validation of ORANI via MACRO and as well furnishes an estimate of the calendar period corresponding to the ORANI short run. The only complications to this story in practice are due to the vector nature of  $y$ , and the need to choose  $t^*$  simultaneously with other parameters of the interface.

#### 4. THE TWO MODEL TYPES

- (a) ORANI ORANI (DPSV (1982)) is a CGE model of the Johansen (1960) class. As we have seen in Section 3.1, under a typical allocation of variables to the endogenous and exogenous categories, a cdcs solution to ORANI can be written

$$y_0 = C_0 z_0 \quad (4.1)$$

where the subscript 0 denotes ORANI variables and parameters;  $y_0$  represents a vector of proportional changes (relative to control) in ORANI endogenous variables;  $z_0$  represents a vector of sustained proportional changes (relative to control) in ORANI exogenous variables, and  $C_0$  is the matrix of ORANI elasticities.<sup>3</sup> The following quotation illustrates the way in which results generated by (4.1) may be interpreted: "given a policy change A, then in the macro-economic environment B, variable C will differ in the short-run by x per cent from the value it would have had in the absence of the policy change" (DPSV (1982), p.63). Implicit in the construction and interpretation of the ORANI elasticity matrix  $C_0$  is the notion of the ORANI short-run,  $t^*$ , which is defined as a period long enough for prices to adjust, for output to be expanded using given plant, for new investment plans to be made and new capital goods to be purchased, but not long enough for the size of capital stock in use to change as a result of the shock. To indicate explicitly the fact that the result (4.1) compares two solutions of ORANI at  $t^*$ , we may write instead

$$y_0(t^*) = C_0(t^*)z_0. \quad (4.2)$$

Thus  $y_0$  is the proportional difference between two equilibria at  $t^*$ . This difference is conditional on the maintenance of the exogenous macroeconomic environment. Variables embodying this environment are represented in  $z_0$  where they are assigned zero values. However the

ORANI variables. Only macroeconomic variables are involved at the interface. A listing of ORANI variables relevant to the interface is given in Table 1. Table 2 shows a similar partial listing of MACRO variables.

From the listings of ORANI and MACRO variables in Tables 1 and 2 respectively it is evident that the following variables are endogenous to both models:

	Double Endogeneities	
	log Yg	Output
	log P	Prices
	log I <sub>H</sub>	Employment
	log i	Imports

A set of variables of particular interest in view of the role of MACRO in endogenizing the macroeconomic environment of ORANI is the following group of ORANI exogenous variables:

	MACRO to ORANI Feedbacks (ORANI Definitions)	
	log E	Exchange Rate
	log (W/P)	Real Wages
	log C <sub>R</sub>	Real Household Expenditure
	log I <sub>R</sub>	Real Gross Private Investment
		(including investment in dwellings)
	log K(0)	Initial Capital Stocks

Variables exogenous to MACRO and endogenized by ORANI are:

	ORANI to MACRO Feedbacks	
	log P <sub>W1</sub>	Price of Wool
	log x	Quantity of Exports
	log P <sub>X</sub>	Price of exports

In practice matters are complicated by the need to select various combinations of MACRO endogenous variables to correspond to the definitions of certain ORANI exogenous variables (for details, see Cooper (1983), pp.12-13).

In the recursive case developed above in which there are no reverse linkages from ORANI to MACRO, the complete ORANI-MACRO system consists of (6.11) and the MACRO solution

$$Y_M(t^*) = C_M(t^*)Z_M \quad (6.12)$$

In this system certain variables will be endogenized both in  $Y_M$  and in  $Y_0$ . The interfacing method consists of choosing the within-short-run-adjustment coefficients vector  $\beta$  and the length of the ORANI short run  $t^*$  which minimize the inconsistencies between the MACRO and ORANI sides of the model.

In the case where there exist variables driving MACRO which are endogenous to ORANI - this occurs in fact (see below) - the same principles are used to interface the models: that is, ORANI is endowed with a within-short-run dynamics conditional on the unknown values of the interface parameters, which are then chosen to minimize inconsistencies in the double endogeneities at  $t^*$ . The formalities of this procedure are set out in Cooper and McLaren (1982).

#### 7. CALIBRATION OF THE INTERFACE PARAMETERS

In sections 5 and 6 we have described an interfacing method that is specific to some injected shock or shocks. Possible approaches to making the procedure operational are:

- (i) the construction of a new interface for each simulation conducted on the O-M system;

- (ii) the selection of interface parameters which optimize a criterion function defined over a nominated set containing a variety of shocks;
- (iii) the selection of a set of interface parameters from a single standard simulation.

We have chosen (iii). In keeping with the literature on the comparative analysis of macrodynamic models (see, e.g. De Bever et al. (1979)), we have chosen an exogenous increase in government spending as the standard simulation.

In considering the interplay between ORANI and MACRO variables it is not necessary to carry the complete (and impossibly long) list of

original shock (i.e., the non-zero elements of  $z_0$ ) may also cause changes in variables outside ORANI (i.e., in MACRO). Some of the latter variables appear among the elements of  $z_0$  which are set to zero in stand-alone applications of ORANI using (4.2). Thus when (4.2) is used alone the implicit assumption is that the induced differentials in the macroeconomic environment are sterilized by offsetting use of fiscal and/or monetary instruments.

(b) MACRO Our MACRO model, MACRO81, is an adaptation (see Cooper (1983)) of the Reserve Bank's RBII model as documented in the appendix to Jonson and Trevor (1981). Underlying it is a first-order stochastic differential equation system which may be written

$$d Y_M(t) = A_M Y_M(t)dt + B_M Z_M(t)dt + dv(t), \quad (4.3)$$

where the subscript M indicates MACRO variables and coefficients, Y and Z are vectors of logarithms of endogenous and exogenous variables respectively, and  $dv(t)$  is a Gaussian vector process. The solution of this system may be written

$$Y_M(t) = e^{A_M t} [Y_M(0) + \int_0^t e^{-A_M \tau} B_M Z_M(\tau)d\tau] \quad (4.4)$$

$$+ e^{A_M t} \int_0^t e^{-A_M \tau} dv(\tau),$$

where  $e^{A_M t}$  is defined by  $P e^{\Lambda T_p} P^{-1}$ , in which P is the matrix containing the characteristic vectors of  $A_M$ , and  $\Lambda$  is the diagonal matrix containing the characteristic roots of  $A_M$ . The matrix  $e^{\Lambda T}$  has typical element  $e^{\lambda_i T}$ , in which  $\lambda_i$  is the  $i$ th characteristic root of  $A_M$ . Let  $\Delta^*(\cdot)$  be the operator taking the differential between  $(\cdot)$  when the exogenous variables follow the shocked path  $[Z_M(\tau) + z_M^*, \tau \in (0, t)]$  and its value at the same point of time when they follow the control path  $[Z_M(\tau), \tau \in (0, t)]$ . Since  $\Delta^*(Z_M(\tau) + z_M^*) \equiv z_M$  for all relevant  $\tau$ , we have

$$\Delta^* Y_M(t) = [e^{A_M t} \int_0^t e^{-A_M \tau} B_M d\tau] z_M \quad (4.5)$$

or

$$Y_M(t) = C_M(t) z_M \quad (\text{say}), \quad (4.6)$$

where

$$C_M(t) = A_M^{-1} [e^{A_M t} - I] B_M. \quad (4.7)$$

The notation on the left of (4.5) emphasizes that the differentials involved are deviations from control at  $t$ . However the notation (4.6) is more convenient and is adopted from hereon. The stochastic term on the right of (4.4) disappears in (4.5) because the introduction of the shock  $z_M$  into  $\{z_M(\tau); \tau \in (0, t]\}$  does not affect the realization of  $v(t)$ . Thus  $\Delta^*$  different alternative realizations of the same sample which differ only in their systematic part.

##### 5. TEMPORAL AGGREGATION

Equation (4.6) demonstrates that, for arbitrary  $t$ , the MACRO model can be written in a Johansen-like form. It is tempting to combine (4.2) and (4.6) into one system. Before this can be accomplished successfully, however, it is necessary to take account of the difference between the time profile of shocks  $z_0$  suitable for input into ORANI and the evolving nature of outputs  $y_M(t)$  ( $t \in (0, t^*]$ ) from MACRO.

In Figure 2a are shown a sustained proportional shock  $z$  in a doubly exogenous variable  $Z$  and the response  $y_M^0(t)$  in time of a variable  $y_M^0$  which is endogenous to MACRO but exogenous to ORANI. (In typical short-run ORANI configurations, the real wage is such a variable.) Considered as an exogenous input to ORANI,  $z$  in Figure 2a is a suitable shock; however  $y_M^0(t)$  is not. Notionally  $y_M^0(t)$  can be split up into a (large) number of step functions; this is shown in Figure 2b. We are interested in the ORANI response at  $t^*$  to the combined stimuli of  $z$  maintained throughout  $(0, t^*]$  and the series of step shocks in  $y_M^0$ , which are maintained for successively shorter and shorter periods as we move from 0 to  $t^*$ . To be able to evaluate the impact of these shocks whose duration is less than  $t^*$  it is necessary to endow ORANI with a within-short-period dynamics. The so augmented model will be referred to as ORANI+.

Then (6.3) can be written more simply as

$$Y_0(t^*) = H B_M Z_M. \quad (6.6)$$

The right-hand side of (6.6) can be expressed in terms of  $Y_M(t^*)$  by the following argument:

$$Y_0(t^*) = H [e^{A_M t^*} - I]^{-1} A_M^{-1} [e^{A_M t^*} - I] B_M Z_M. \quad (6.7)$$

Thus from (4.6) and (4.7)

$$\begin{aligned} Y_0(t^*) &\equiv H [e^{A_M t^*} - I]^{-1} A_M^{-1} Y_M(t^*) \\ &= G Y_M(t^*) \quad (\text{say}) \end{aligned} \quad (6.8)$$

The coefficient matrix  $G$  in (6.8) gives the effects at  $t^*$  on the ORANI endogenous variables of the shocks endogenized by MACRO as evaluated at  $t^*$ .  $G$  can be thought of as an operator which corrects the timing of these MACRO variables to make them suitable inputs to ORANI and then performs the required multiplication.

Let  $S$  be a selection operator analogous to  $R$  in (6.4) such that putting

$$\begin{aligned} z_0 &= Sz \quad (6.9) \\ \text{produces an ORANI shock vector containing zeros except for the doubly exogenous shocks which take on their values as in } z. \quad \text{The initial doubly exogenous shock } z \text{ produces in ORANI a direct effect } C_0 S z \text{ and an indirect effect } G C_M(t^*) = G C_M(t^*) R z. \quad \text{The total ORANI response is obtained by adding these:} \end{aligned}$$

$$Y_0(t^*) = C_0 S z + G C_M(t^*) R z. \quad (6.10)$$

In the case where the initial shock is not confined to double exogeneities (but in which the shocks  $z_0$  and  $z_M$  contain no contradictions), (6.10) generalizes to

$$Y_0(t^*) = C_0 z_0 + G C_M(t^*) z_M. \quad (6.11)$$

$$y_M^0(t) = \int_0^t \frac{dy_M^0(\tau)}{d\tau} d\tau. \quad (6.1)$$

Each of these derivatives may be interpreted as an infinitesimal shock to ORANI sustained over the interval  $[\tau, t]$ . Let  $L$  be the linear operator which, when operating on  $y_M^0(t)$ , produces a vector conformable with  $z_0$ , having as its elements the values of the appropriate elements of  $y_M^0(t)$  in positions corresponding to ORANI exogenous variables endogenized by MACRO, and zeros elsewhere. Then  $d(Ly_M^0(\tau)) \equiv L dy_M^0(\tau)$  is a shock in a form suitable for acceptance by ORANI+. Inject these instantaneous shocks for  $\tau \in (0, s]$  into ORANI+ via (5.1); given the linearity of the model, the accumulated response at  $s, s \in (0, t]$ , is obtained by summation:

$$\begin{aligned} y_0(s) &= \int_0^s C_0(s-\tau) L dy_M^0(\tau) \\ &= \int_0^s C_0(s-\tau) L Q dy_M^0(\tau), \end{aligned} \quad (6.2)$$

where  $Q$  is the linear operator that selects the subset  $y_M^0(\tau)$  from  $y_M^0(t)$ . Using (4.6), (4.7) and (5.2) in (6.2), we obtain for  $s=t^*$

$$y_0(t^*) = \int_0^{t^*} A_0^{-1} [e^{A_0(t^*-\tau)} - I] B_0 L Q e^{A_M \tau} d\tau B_M z_M. \quad (6.3)$$

This is the ORANI+ response at  $t^*$  (i.e., the ORANI response) to the variables exogenous to it which respond endogenously in MACRO to the shock  $z_M$ . If  $z$  is the initial shock in the double exogeneities, then in (6.3)  $z_M$  can be replaced by

$$z_M = Rz, \quad (6.4)$$

where the operator  $R$  produces a vector conformable to  $z_M$  having as its elements the elements of  $z$  where possible, and zeros elsewhere. Given the assumption (5.3) on  $A_0$ , and given the value of  $C_0 (\equiv C_0(t^*))$  from ORANI, for any  $\beta$  vector and value of  $t^*$  we can compute  $B_0$  from (5.2). Hence the integral term in (6.3) can be computed (see Cooper and McLaren (1980), p.26 and (1982) p.16 for the details). Let its computed value be

$$\int_0^{t^*} A^{-1} [e^{A_0(t^*-\tau)} - I] B_0 L Q e^{A_M \tau} d\tau = H \quad (\text{say}). \quad (6.5)$$

Figure 2a. The shock  $z$  in a doubly exogenous variable  $z$  is injected into MACRO at  $t=0$ .  $t^*$  is the length of the ORANI short run. The proportional response in the MACRO endogenous variable  $y_M^0$  is  $y_M^0(t)$ . ORANI will accept shocks in the step-function form displayed by  $z$ ; it cannot accept an arbitrarily evolving shock such as that displayed by  $y_M^0(t)$ .

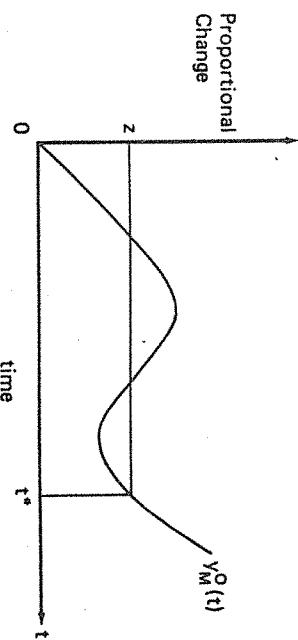
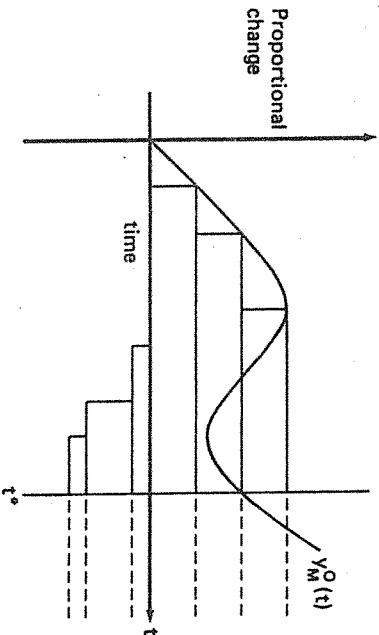


Figure 2b. The log differential  $y_M^0(t)$  is endogenous to MACRO but appears also as an exogenous input into ORANI. The continuously varying shock  $y_M^0(t)$  can be represented as a sequence of discrete step-function shocks as shown.



The dynamics in ORANI+ is kept as simple as possible. For each of a small, but exhaustive, number of classes of endogenous variables in ORANI+, it is assumed that the within-short-run response belongs to a one parameter family. Given (4.7) it is natural to assume (by analogy with MACRO) that the ORANI+ endogenous responses at  $s, s \in (0, t^*)$ , take the form

$$y_0(s) = C_0(s)z_0, \quad (5.1)$$

where

$$C_0(s) = A_0^{-1}[e^{A_0 s} - I]B_0. \quad (5.2)$$

From ORANI the right-hand matrix in (5.2) is known only for  $s=t^*$ . Simplifying assumptions about the structure of  $A_0$  are therefore needed.

We assume that  $A_0$  is of the form

$$A_0 = (\ln \beta)I, \quad (5.3)$$

where  $(\ln \beta)$  is a diagonal matrix which, in the application reported below, has only six distinct elements. Let  $(\ln \beta_i)$  be the  $i$ th such distinct value, and let  $y_{0j}(\tau)$  be the cdfs solution for the  $j$ th ORANI endogenous variable, which is assigned the within-short-run adjustment parameter  $\beta_i$ . Then our assumptions imply

$$y_{0j}(\tau) = \frac{\beta_i^\tau - 1}{\beta_i^{t^*} - 1} y_{0j}(t^*), \quad 0 < \tau < t^*. \quad (5.4)$$

Possible within-short-run adjustment paths are shown in Figure 3. Notice that since this dynamics applies only within the short-run, values of  $\beta_i > 1$  are admissible, and  $\beta_i$  values in general bear no necessary relation to long-run-stability conditions. Indeed, adjustment paths such as (e) in Figure 3 give well with some allegedly realistic descriptions of the adjustment of variables (such as prices of manufactures) which cannot be changed costlessly.

## 6. THE INTERFACING METHOD

The interface parameters of the ORANI+ MACRO system are the length of the ORANI short run,  $t^*$ , and the adjustment parameters  $\beta_i$ . The two models are to be interfaced with these parameters set initially to arbitrary values. A search procedure is then used to optimize their

values. In what follows the various coefficient matrices in the system are all known up to an arbitrary specification of  $t^*$  and the vector of  $\beta$  values. We start with the assumption that the system is recursive; that is, while we allow ORANI to be driven by variables that are endogenized in MACRO, we assume initially that there are no MACRO exogenous variables endogenized by ORANI.

Consider again the evolution of  $y_M^0(t)$  in Figure 2b. Suppose now that this is the path of just one of many such variables; i.e., redefine  $y_M^0(t)$  to be vector of exogenous inputs into ORANI which are endogenized in MACRO. In order to take an infinitesimal rather than a discrete step-function decomposition of  $y_M^0(t)$ , write it as the integral of its own derivatives:

Figure 3. Within short-run dynamics in ORANI.  $t^*$  is the ORANI short run. The within-short-period dynamics in ORANI for an endogenous variable with adjustment coefficient  $\beta_i$  is shown for different values of  $\beta_i$ . The point A is the short run contemporaneous differential comparative static solution for ORANI at  $t^*$ . The adjustment paths in  $(0, t^*)$  imply nothing about long run dynamics.

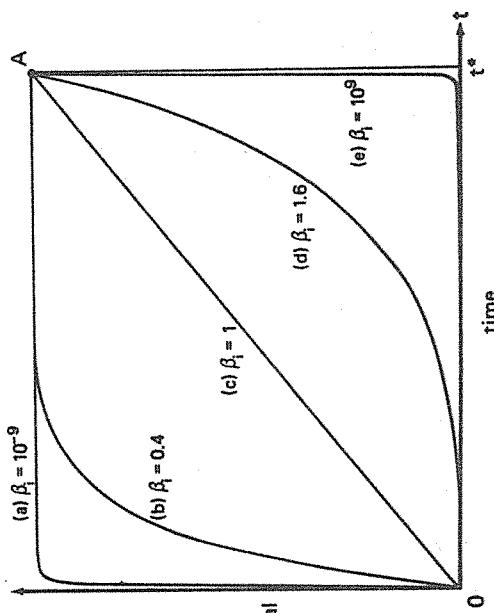


Figure 3. Within short-run dynamics in ORANI.  $t^*$  is the ORANI short run. The within-short-period dynamics in ORANI for an endogenous variable with adjustment coefficient  $\beta_i$  is shown for different values of  $\beta_i$ . The point A is the short run contemporaneous differential comparative static solution for ORANI at  $t^*$ . The adjustment paths in  $(0, t^*)$  imply nothing about long run dynamics.