

Impact

Project

Impact Research Centre, Baldwin Spencer Building (2nd floor)
The University of Melbourne, PARKVILLE Vic. 3052 AUSTRALIA

Telephone : (03) 344 7417 (from overseas: 61 3 344 7417)

Telex: AA 35185 UNIMEL

Telegrams: UNIMELB, PARKVILLE

Fax: (03) 347 7539 (from overseas: 61 3 347 7539)

The Reconciliation of Computable General Equilibrium and Macroeconomic Modelling: Grounds for Hope?

by

Bruce F. PARSELL

Institute of Applied Economic and Social Research

Alan A. POWELL and Peter J. WILCOXEN

Impact Project Research Centre

University of Melbourne

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Abstract

In the aftermath of the rational expectations debate and the onslaught of the New Classical economics, some builders of macroeconometric models have begun to change some of their habits, arguably for the better. In particular, neoclassical discipline is increasingly respected in the formulation of the steady states or balanced growth solutions of the latest versions of several models (e.g., Australia's Murphy Model, and the McKibbin-Sachs Global Model). As well, the behaviour of certain variables (especially exchange rates and investment) increasingly tends to be linked to intertemporal optimization. In this paper we evaluate these innovations and illustrate the role of each, using recent simulations of the Murphy and McKibbin-Sachs models. We conclude that conditions have never been better for convergence in the two streams of economy-wide modelling.

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THE RECONCILIATION OF COMPUTABLE GENERAL EQUILIBRIUM AND MACROECONOMIC MODELLING: GROUNDS FOR HOPE?¹

by

Bruce F. PARSELL, Alan A. POWELL and Peter J. WILCOXEN²

University of Melbourne

1. Introduction

The recent trend towards reconstructing macroeconomics on an explicit foundation of microeconomic behaviour³ promises great improvements in the quality and consistency of economy-wide economic models. Until recently, most large models could be categorized as principally either macroeconomic or microeconomic. Macro models have typically been collections of loosely related regression equations carefully fitted to historical data. Often the equations are not closely linked to optimizing behaviour, and include a large number of lagged variables. Typical members of this set are the Wharton model⁴, and the Australian Treasury's NIF88 model.⁵

In contrast, microeconomic models are usually painstakingly derived from explicit optimization problems. Often, however, their link to empirical data has been weaker than for macro models; consequently, their ability to track historical time series — at least, within the time period used to estimate the model's parameters — is somewhat worse. Moreover, micro models usually include only behaviour that can be derived from optimization of reasonably straightforward problems, and so they may miss some of the linkages picked up by the reduced-form approach used by macro modellers. Belonging to the microeconomically oriented group are virtually all CGE models,⁶ including, for example, those of Ballard, Fullerton, Shoven and Whalley (1985), Dervis, De Melo and Robinson (1982), Deardorff and Stern (1986), Dixon, Parmenter, Sutton and Vincent (1982), Hudson and Jorgenson (1974), and Ginsburgh and Waelbroeck (1981).

¹ This paper was first presented at the Fourth Meeting of the *Taskforce on Applied General Equilibrium Modeling* held at the International Institute for Applied Systems Analysis, Laxenburg, Austria, in August 1989; it draws heavily on our paper (Parsell, Powell and Wilcoxen, 1991) prepared for the Australian National University-Treasury Conference on *Fiscal Policy and the Current Account*, held in Canberra on 5-6th June 1989.

² We are grateful for the assistance of Warwick McKibbin and Chris Murphy in providing detailed explanations of their models and simulation results. Chris Murphy kindly also gave us comments on earlier drafts of this paper. Neither is, of course, responsible for any errors remaining.

³ For example, consumption theories based on the permanent income hypothesis, or investment models driven by the marginal variant of Tobin's q .

⁴ See Intriligator (1978), pp. 441-444, for a brief description of the Wharton model, and for relevant citations.

⁵ See Simes (1988) and Simes *et al.* (1988), and the series of working papers cited therein.

⁶ In this paper we make no distinction between *applied* and *computable* general equilibrium, using *CGE* as a convenient abbreviation.

In this paper we take up a theme explored by one of us (Powell, 1981) in reflecting on what transpired about a decade ago at the National Science Foundation/National Bureau of Economic Research conference on large-scale macroeconomic modelling (held in Ann Arbor, Michigan). That theme is the scope for reconciliation of the different approaches to economy-wide modelling. As we shall see, more optimism is warranted now than then.

Two exemplars of the new paths being taken by applied macroeconomists will illustrate our explorations below. The first of these is the McKibbin-Sachs Global Model (MSG2), a world model which includes Australia as one of its regions.⁷ MSG2 is fundamentally a micro model because almost all of its equations are derived from optimization. It does, however, include a number of features from macroeconomics, including sticky wages and a money demand equation lacking a Walrasian pedigree.

The second model used to illustrate our arguments is the Murphy Model of the Australian economy (MM).⁸ MM is fundamentally a macro model because many of its key equations are not derived from optimization and include somewhat arbitrary lag structures. On the other hand, it is not a typical macro model because it includes an underlying microeconomic structure that determines its long-run behaviour.

In the remainder of this paper, we start in Section 2 with a brief account of the main thrust of the open-economy macroeconomics of the 'eighties. The material is extensively borrowed from Turnovsky (1989). Then, in Section 3, we give a brief account of the two applied macro models mentioned above, which, to varying degrees, incorporate the insights of the new macro theories. The key ideas, it will turn out, are *intertemporal optimization* and at least some use of *rational expectations* in model construction. In Section 4 we give a very brief summary of the tracking behaviour of MSG2 and MM in a simulation of an unanticipated, temporary, 'bond-financed' period of fiscal restraint. Section 5 contains our concluding remarks.

2. The Open-economy Macroeconomic Theory of the 'Eighties

In this section, we lean heavily on an invited lecture to the Econometric Society by Turnovsky (1989), who characterizes the open-economy macro theory of the 'eighties as being

'based much more on intertemporal optimization of representative agents in the economy.'⁹

A stylized or core model capturing the essence of the new paradigm developed in the papers surveyed by Turnovsky is set out in his paper.¹⁰ It is a continuous-time model recognizing two goods (domestic and foreign) and four

⁷ McKibbin and Sachs (1991), McKibbin (1988), McKibbin and Elliot (1989), McKibbin and Sieglhoff (1988a & b).

⁸ Murphy (1989a & b, 1988a & b).

⁹ The available documentation [Turnovsky (1989)] comes as a skeletal handout, rather than a fully fleshed out paper. The class of models reviewed, however, is well represented in Sen and Turnovsky (1989a & b).

¹⁰ *Op. cit.*

representative agents: a consumer, a producer/ investor, the domestic government, and an arbitrager.

2.1 The Consumer and the Government

The (infinitely lived) **consumer** maximizes the present value of a utility stream generated at any instant of time by the rate at which private purchases of the two commodities are being consumed, by the rate at which the government is providing publicly purchased supplies of them, and by the rate at which leisure is being consumed. The consumer's time-preference discount rate is a constant (b).

In the simplest version of this core paradigm, only consumers borrow abroad.¹¹ They issue bonds, whose stock (measured in terms of the foreign good) is denoted by $-b$; they use increases in debt outstanding ($\dot{b} < 0$) to finance any temporary short-fall between expenditure and income. The foreign real interest rate, i^* , remains unaffected by these transactions, regardless of their size.

The **government** simply collects a lump-sum tax T which it spends on publicly providing g_x units of the domestic good and g_y units of the foreign good. Unlike the other agents in the model, no explicitly optimal behaviour is attributed to the government. With x and y denoting the consumer's purchases of the domestic and imported good, respectively, p denoting income from capital, L the amount of labour supplied,¹² w the wage rate, and s the market rate at which the domestic good exchanges for the foreign good,¹³ the *representative consumer's problem* can be stated as:

$$(1) \quad \text{Max} \int_0^{\infty} [U(x,y) + W(g_x, g_y) + V(h - L)] e^{-bt} dt ;$$

subject to:

$$(2) \quad \dot{b} = \frac{1}{s} [wL + p - x - sy + si^* b - T] ,$$

with initial condition:

$$(3) \quad b(0) = b_0 ,$$

and transversality condition:

¹¹ Turnovsky (*ibid.*) does allow the government to borrow, binding it by an intertemporal budget constraint. For simplicity, we abstract from this detail in the account given here.

¹² In what follows, the upper limit on time that potentially could be worked is denoted by h , so that $(h-L)$ is leisure.

¹³ s has as units the number of units of domestically produced commodity which exchange for one unit of foreign commodity; i.e., $s = fp_y/p_x$ where p_y and p_x respectively are the prices of the foreign and of the domestic commodity and f is the exchange rate (\$A per foreign \$).

$$(4) \quad \lim_{t \rightarrow \infty} b(t) e^{-i^*t} = 0 .$$

Equation (2) equates new debt issue with the excess of private spending ($x + sy$) and debt servicing ($-si^*b$) over private disposable income ($wL + p - T$); equation (3) simply states that the net foreign assets held by the domestic consumers has a given value b_0 at the beginning of the plan formulated at $t = 0$; while the terminal condition (4) ensures that the present value of such wealth (or, if negative, debt) cannot become unbounded over the (infinitely long) lifetime of the consumer.

2.2 The Producer/Investor

The task of the representative producer/investor is to maximize the present value of the domestic firm. Central to his/her problem is a function $C(I)$ described by Turnovsky as "the installation costs associated with the purchase of I units of new capital". The excess of $C(I)$ over the amount of new capital I put in place is the familiar *adjustment cost* idea developed by Eisner and Strotz (1963), Treadway (1969), Lucas (1967), Gould (1968) and others, and given a modern perspective by Hayashi (1982) and Abel and Blanchard (1983). The production function for gross output is written $F(k,L)$, while the instantaneous domestic market rate of interest is denoted $i(t)$.

In this notation the producer/investor must solve the following problem:

$$(5) \quad \text{Max} \int_0^{\infty} [F(k,L) - wL - C(I)] e^{-\int_0^t i(t)dt} dt ;$$

subject to the accumulation identity:¹⁴

$$(6) \quad \dot{k} = I ,$$

and the initial condition:

$$(7) \quad k(0) = k_0 ,$$

plus a suitable transversality condition, such as:

$$(8) \quad \lim_{t \rightarrow \infty} q k e^{-\int_0^t i(t)dt} = 0 ,$$

which states that if valued at the marginal value q of a unit of new capital, the capital stock does not grow faster than the domestic interest rate. Instantaneous cash flow at t [the integrand (before discounting) in (5)] is kept linearly homogeneous by requiring F and C to be homogeneous of first degree in the vector (L, k, I) .

¹⁴ For simplicity, depreciation is set to zero in Turnovsky's core model.

2.3 Arbitragers and Uncovered Interest Parity

The role of the final agent, the **arbitrager**, is to ensure that the nominal domestic interest rate exceeds the exogenously given foreign rate exactly to the extent that the domestic currency is expected to depreciate against the foreign currency: that is, uncovered interest parity prevails:

$$(9) \quad \left(i + \frac{\dot{p}_x}{p_x}\right) = \left(i^* + \frac{\dot{p}_y}{p_y}\right) + e;$$

where \dot{p}_x/p_x and \dot{p}_y/p_y , respectively, are the domestic and foreign inflation rates, and e is the time rate (e.g., proportion per annum) at which the domestic exchange rate is expected to depreciate.¹⁵ Rational expectations arise in some form in most of the open-economy macro-theoretical models of the 'eighties; they also hold for agents in financial markets in the applied models MSG2 and MM. Thus (9) holds at every instant in *planning* time, where e is a model-consistent forecast of the rate of domestic exchange rate depreciation. Moreover, if no new shocks are injected after the initial instant at which plans are made, then these model-consistent forecasts are realized in simulations of the MSG2 and MM models over *actual* time.

2.4 A Glimmer of Hope

The above framework, with or without an explicit (but if explicit, *ad hoc*) treatment of demand for a monetary asset, is sufficient to characterize what Turnovsky describes as a *macroeconomic equilibrium*. However, with the possible exceptions of (i) the high degree of aggregation, (ii) the *ad hoc* treatment of money demand, and (iii) the non-explicitly-optimizing behaviour of the government, there is no reason to differentiate it from an intertemporal general equilibrium model. This leads us to conjecture that the models currently used by macroeconomic theorists, if adopted as the basic paradigm by applied modelling practitioners, will yield a Walrasian macroeconomics. This is because the new models:

- (a) build up a picture of macroeconomic 'equilibrium' from explicit statements about the objective functions of various agents;
- (b) respect the budget constraints faced by these agents;
- (c) being macro models, and therefore having to deal with at least one asset, necessarily involve intertemporal optimization by one or more agents within them;
- (d) will, because of (c), have dynamic properties that flow from their theoretical specification, rather than from *ad hoc* lag distributions.

It would be foolish, however, to conclude that macrotheorists' motivation for treading this new road spring from an admiration of CGE modellers' efforts. Rather, they were forced in that direction by the rise of rational expectations theory and by the publication of the Lucas critique (Lucas, 1976). Although closely related, these were somewhat separate events since the point made by

¹⁵ Although interest parity conditions are very popular with modellers, the empirical evidence for them remains inconclusive. See Fischer *et al.* (1989).

Lucas applies to all reduced-form macroeconomic models, regardless of whether or not expectations are, in fact, rational.

Adopting the intertemporal optimization framework, however, entails a substantial cost: it becomes necessary to specify exactly what agents expect about certain variables far into the future. Ideally, this requires formulating and estimating an explicit model of how expectations are formed. Unfortunately, it is usually impossible to observe expectations directly, so little empirical progress has been made in that line of research. Moreover, there are few formulations of the expectations mechanism that are not completely *ad hoc*. As a result, one simplification that has often been adopted is to assume that agents have perfect foresight. Much of the impetus behind this comes from the theoretical appeal of the rational expectations hypothesis.

Increasingly, applied macro modellers are following the new paradigm, at least in part. A leading example is MSG2. Surprisingly, it is not necessary to go all the way to fully explicit intertemporal optimization to harness much of the power of the new paradigm. In MM, Chris Murphy concentrates just on ensuring that a well-defined balanced growth path exists, and that MM converges to it from arbitrary starting values. As noted above, forward-looking behaviour applies in MM's financial markets, where expectations are model-consistent. Although not yet intertemporal, optimizers are becoming more frequent in current versions of the London Business School (LBS) Model¹⁶ and the Fair Model¹⁷, which go some of the way down the route taken by Murphy.

3. Salient Features of Two New Applied Macro Models: MSG2 and MM¹⁸

In many respects MM and MSG2 are very similar. As we have seen above, the key features which distinguish them from other applied macro models are:

- (i) forward-looking agents in financial markets who know and use the model's projections of all future exchange and interest rates;
- (ii) uncovered interest parity (UIP) linking exchange rates and interest rates;
- (iii) governments constrained by intertemporal budget constraints; and
- (iv) the existence of a well-defined neoclassical balanced growth path towards which the simulated economy converges after transitory disturbances brought about by an exogenous shock.

Differences between the models are evident mainly in the specification of short-run dynamics. MM includes a number of lags which lead to slower (and often oscillating) adjustments to shocks. These lagged terms are estimated in the Wharton tradition: various structures are tested in search of a specification producing good within-sample test statistics. MSG2, on the other hand,

¹⁶ Holly, Dinenis, Levine and Smith (1988).

¹⁷ Fair (1984).

¹⁸ In this and the next section we draw extensively on Parsell, Powell and Wilcoxon (1991).

includes lagged adjustment only in the determination of wages¹⁹. Other major differences and similarities between MM and MSG2 are displayed in Table 1. For later reference we note that the tax instrument involved in the simulations reported here is a lump-sum tax.

Notwithstanding MM's cyclical short-run response to shocks, capital and output adjust flexibly in the long run to reestablish an exogenously given (world) real rate of return. In fact, MM has a well-defined and neoclassically interpretable long-run growth path to which it converges after its transient (and often cyclical) responses work themselves out. Whilst this limiting steady-state growth path would be consistent with intertemporal optimization by agents, this is not its genesis in MM²⁰; rather a balanced growth path is simply imposed. Considerable ingenuity is then needed to ensure that the short-run dynamics of the system as estimated guarantee convergence to this limiting path.

In MSG2, on the other hand, some consumers, some investors, and all agents of a special class called export facilitators are modelled as intertemporal optimizers. The latter maximize the present value of net revenue subject to penalties which are incurred when the flow rate of exports changes. Given that the domestic good in MSG2 is a perfect transformate of the exportable, such costs are necessary to make plausible the model's export response.

In both models, rational expectations apply to those agents specified to be intertemporal optimizers; i.e., to arbitragers in MM, and in MSG2 also to export facilitators and to some investors and some consumers.

4. An Illustrative Simulation with MSG2 and MM²¹

4.1 The Shock

The shock used to illustrate the behaviour of the models is a two-percentage-point reduction in the share of government spending in GDP

¹⁹ However, many of the parameters in MSG2 were taken from the literature, while the remainder were chosen arbitrarily. None of the parameters were estimated specifically for the model.

²⁰ The only intertemporally optimizing agents in MM are arbitragers operating in financial markets.

²¹ A more comprehensive account is available in Parsell, Powell and Wilcoxon (1991).

Table 1
A Brief Comparison of the Murphy and MSG2 Models

Attribute	Murphy Model	MSG2 Model
Size	94 eqns in about 136 variables (eqns include 77 identities)	approx. 60 eqns in 79 variables per fully modelled ^b entity: Total of about 260 eqns in 328 variables
Scope	One country (Australia)	Four countries (Australia, U.S., Japan, Germany) plus four <i>groups of countries</i> (the rest of the EMS, the rest of the OECD, non-oil LDC's and OPEC)
Focus	General macro policy issues for Australia, short- and medium-run forecasting	Macro interactions among national economies, policy analysis for a single country
Time Unit	Quarter	Year
Steady State ^a	Exists; along neoclassical lines	As for Murphy
Model-consistent Expectations	Important in determining the exchange rate and the bond rate	As for Murphy; model consistent expectations are also important in MSG2 in determining the targets towards which exports adjust, and in determining (parts of) consumption and investment
Uncovered Interest Parity	An important mechanism	As for Murphy
Special treatment of:		
Oil	No	Yes
Housing	Yes	No
Technical change ^c	Harrod-neutral (0.81 per cent per year)	Harrod-neutral (1.0 per cent per year)
Labour force growth ^c	1.7 per cent per annum	2 per cent per annum

^a Strictly speaking, 'asymptotic balanced growth path'.

^b For LDCs and OPEC, only current and capital accounts are modelled. The sum of the Harrod-neutral rate of technical change and the rate of labour force growth gives the steady-state growth rates of the models; namely, 2.51 and 3 per cent per year for Murphy and MSG2, respectively.

Source: Parsell, Powell and Wilcoxon (1991).

maintained for five years. Tax rates, except as noted below, were fixed; and so the cut in spending lowered the government's budget deficit. The share of government spending in GDP returned to its original level after five years. Although initially unanticipated, once the government's plans were announced agents did expect the rebound in public spending after five years. With some abuse of terminology, we find it convenient to refer to this shock as a *credible, unanticipated, temporary, bond-financed, fiscal contraction*.

4.2 The Main Results

Given Australia's size in the world economy, other entities in MSG2 are hardly affected by the change in Australian fiscal policy. Hence we report only the effects on the local economy. The principal results for both models are summarized in Charts 1–4.

Central to understanding the projections is the behaviour of the exchange and interest rates. Both models give qualitatively similar trajectories for these variables (Chart 3), the principal difference being the presence of damped cycles in the MM results. Both show an initial depreciation of the Australian dollar against other currencies. This reflects the operation of uncovered interest parity (UIP), which equates the (correctly) anticipated time rate of change in the foreign currency value of the Australian dollar (per cent per year, say) to the percentage point interest differential prevailing between Australia and the rest of the world. The world interest rate remains unaffected by the domestic fiscal contraction, and so the deviation from control of the time rate of change of the exchange rate (\$ foreign per \$A, per annum) must equal the deviation from control of the Australian short-term interest rate (percentage points per annum).

4.3 Short-run Effects

The fiscal contraction has two direct effects. First, the cut in spending reduces the demand for domestically made and imported commodities. Second, it reduces the budget deficit. These initial direct effects induce a number of other changes in the economy.

As a result of the initial reduction in the government's demand for domestically produced goods, in both models output falls relative to *ceteris paribus*. The money demand functions in MM and MSG2 reflect a transactions motive for holding money. With output falling, the transactions demand for money declines. Since the money supply is fixed, in both models the short-term interest rate has to fall to ensure the that demand matches supply.

²² 'Short-term' here means the rate applicable to a loan whose term is equal to the period of account of the model; i.e., three months for MM and one year for MSG2.

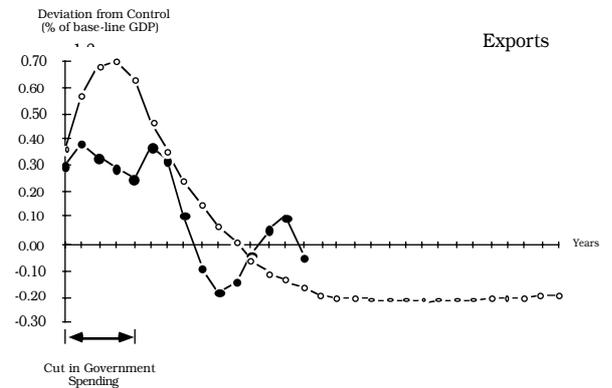
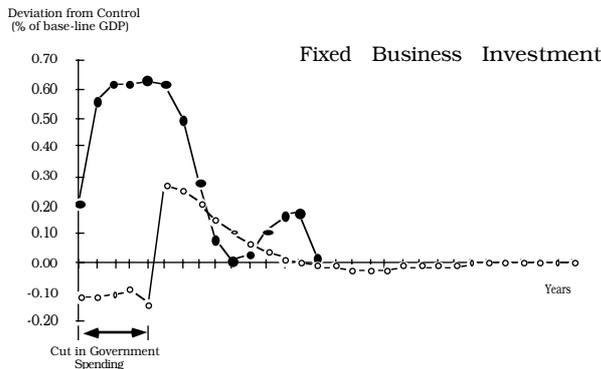
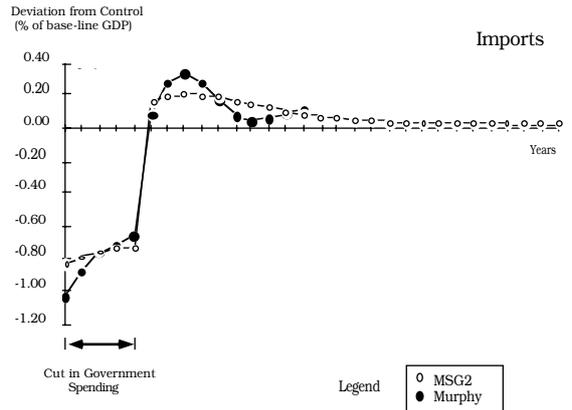
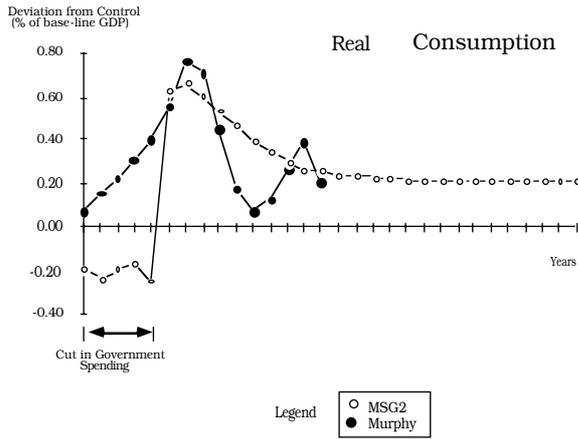


Chart 1: Top panel -- Simulated time path of real consumption
Bottom panel -- Simulated time path of real fixed business investment

Chart 2: Top panel -- Simulated time path of imports
Bottom panel -- Simulated time path of exports

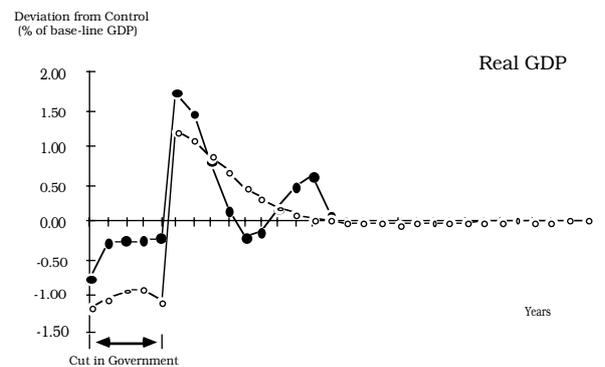
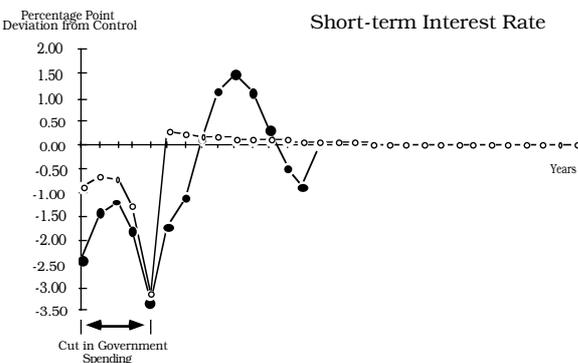
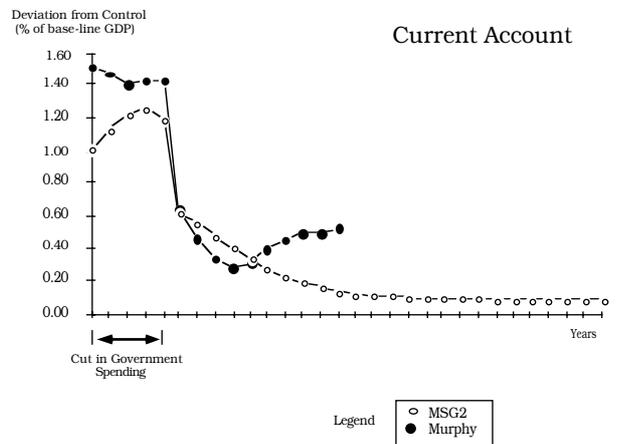
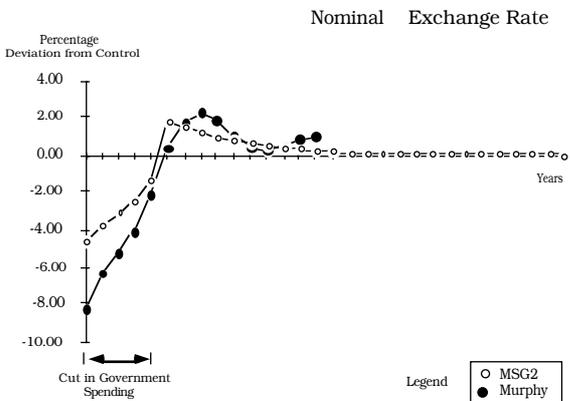


Chart 3: Top panel -- Simulated time path of the nominal exchange rate
Bottom panel -- Simulated time path of the short-term interest rate (3 months for MM, 1 year for MSG2)

Chart 4: Top panel -- Simulated time path of the Current Account
Bottom panel -- Simulated time path of real GDP

Consistent with the much greater initial drop in the exchange rate in MM, the percentage point fall in the interest rate in MSG2 is much smaller than in the former model. Because the change in government demand is known to be temporary, after the initial drop the exchange rate appreciates rapidly in both models.

By the time that government demand returns to its initial value (namely, year six), the exchange rate must have recovered to a level approximately the same as its initial value. Hence the larger the initial drop, the faster the subsequent appreciation. This maxim is substantiated by the MM and MSG2 results (Chart 3). In both models the anticipated appreciation leads to capital inflow as foreigners respond to the higher effective rate of return on Australian assets.

4.4 The Long Run

A consequence of the operation of uncovered interest parity is that transient shocks (like the one analyzed here) can have permanent effects.²³ In particular, the temporary fiscal contraction lowers the long-run ratio of government debt to GDP. All interesting long-run results in both models can be traced to this cause. With tax rates unchanged, the drop in government spending during years 1 through 5 entails smaller budget deficits and slower accumulation of debt. The lower ratio of government debt to GDP in MSG2's balanced growth equilibrium produces only a few other changes in this equilibrium. In the case of MM, the effects are quantitatively somewhat larger, but the qualitative story underlying them is almost exactly the same.

To understand why there is so little effect, it is helpful to consider what would happen if all government bonds were held domestically, and there were no long-run growth in the economy. Under these conditions a drop in the stock of bonds would have no effect whatsoever. To see why this is so, consider what happens to consumers in MSG2. Some 30 per cent of them choose each period's consumption to solve an intertemporal optimization problem.²⁴ For them, changes in consumption are determined by what happens to their wealth. On the one hand, fewer government bonds entail lower wealth since bonds are one of the assets held by consumers. On the other hand, individuals deduct from total wealth the present value of the lump sum tax used to finance interest payments on the bonds. Fewer bonds mean lower taxes, so wealth tends to rise. Thus, *prima facie*, the change in wealth relative to control is ambiguous. However, in this rational expectations world in which governments respect

²³ The occurrence within the models surveyed by Turnovsky (*op. cit.*) of the phenomenon of temporary shocks causing permanent effects is traced by him to differential equations having a zero root. This singularity is associated by Turnovsky with the operation of uncovered interest parity in a paradigm which elsewhere requires *both* the time preference discount rate and the foreign real interest rate to be exogenous. With Fisherian equilibrium requiring (for the existence of the steady state) that the real domestic interest rate and the time preference discount rate be equal, a zero root in the equation of motion for the marginal utility of consumption is implied.

²⁴ The percentage of intertemporally optimizing consumers is a parameter set by the user of MSG2.

their intertemporal budget constraints, Ricardian equivalence operates, and the present value of future lower tax collections in the steady state exactly offsets the drop in wealth due to the lower stock of bonds on issue. Since wealth does not change, neither does consumption.

For the 70 per cent of consumers who are liquidity-constrained, consumption is always equal to income. Reducing the stock of government bonds affects their income in two ways. Since they own bonds, smaller interest payments from the government cause their incomes to fall; however there is a simultaneous drop in the lump-sum tax. The lower income from bonds and the smaller tax collection from current income exactly off-set each other, so again there is no net effect on income or consumption in the steady state. Thus, when all government debt is held domestically, a reduction in bonds will change the composition of income and wealth, but that is all.

In the actual models, however, some of the government bonds are held by foreigners. This changes the results somewhat, causing the drop in government debt to have an effect on the economy. The key fact is that domestic residents pay the *entire* lump sum tax, but receive only a *fraction* of the interest payments. When the stock of bonds drops, consumers' tax burden falls more than their income, so they gain by the amount of interest that would have been paid to foreigners. As in the case described above, both the optimizing and liquidity-constrained consumers increase consumption to reflect the rise in income. It turns out that total consumption rises by $-rDB_f$, (where DB_f and r respectively are the change in foreigners' holdings of Australian bonds and the interest rate), regardless of the ratio of liquidity-constrained to unconstrained consumers.

This increase in steady-state consumption must be exactly matched by an increase in the trade deficit which brings the current account back into balance (causing the foreign debt to GDP ratio to stabilize). Since the increase in consumption and the drop in the balance of trade are equal, there is no change in demand for domestic output, and hence no change in prices or interest rates. This, in turn, keeps investment at its original share of GDP. Finally, since the fiscal contraction was only temporary, government spending also returns to its original share of GDP. Thus, the only long-term consequence of the shock is the reallocation of output from exports to consumption. Temporary restraint now enables a higher standard of living in the long run, according to the models. Introducing growth makes the details slightly more complex, but does not change the basic result.

5. Concluding Remarks

Macroeconomic theorists in the 'eighties have espoused intertemporal optimization by explicitly identified budget-constrained agents as the paradigm of choice. Increasingly, CGE modellers are formulating their models intertemporally.²⁵ If the applied macro practioners follow the lead of their theoretically inclined confreres, the gap between the two schools will narrow rapidly. At least two current applied macro models of which we are aware have adopted all, or a substantial part of the new paradigm; namely, the McKibbin-Sachs Global Model (MSG2) and Australia's Murphy Model (MM). However,

²⁵ Some examples are Feltenstein (1983), Goulder and Summers (1989), Adams (1988), and Jorgenson and Wilcoxon (1989) .

they still differ from most micro models because they have stylized money demand equations, sticky wages, and limit the short-run response of exports. Each of these features can be viewed as a judgement about the extent to which departures from strict Walrasian orthodoxy are needed to secure empirical realism, at least with the current generation of models.

Reconciling believable microeconomic specifications with empirical data is a major obstacle in integrating micro- and macroeconomics. For example, consider the problem of investment: q -theoretic models provide a sound, rigorous formulation but usually fit the data very poorly.²⁶ A modeller is forced, therefore, to choose between micro foundations and statistical fit. Macro models, with their extensive lag structures and loosely specified functional forms, could be regarded as data without theory: they provide a good fit without producing much explanation. Pure micro models have the opposite problem — they often tend to be theory without data.

It would be tempting to insist that models must only incorporate behaviour derived from optimization. Unfortunately, the lack of empirical support for many of the micro theories now used as the foundations of macroeconomics indicates that those specifications fail to capture some important mechanisms at work in actual market economies.²⁷ Until the empirical performance of models based strictly on optimization is greatly improved, there will be some circumstances in which it will continue to be useful to use reduced-form equations for certain variables.²⁸

However, the problems with introducing reduced-form equations are many: it becomes much more difficult to explain why the results of a simulation look the way they do, and virtually impossible to assess the relative merits of different models; finally, their introduction provides an almost unlimited opportunity to indulge in data mining. Nevertheless, there remains a limited role for specifications not explicitly derived from optimization in the provision of forecasts and in other inputs to policy making.

Be that as it may, the intertemporal optimizing macrotheoretical models developed during the 'eighties are pushing applied macro practitioners toward using progressively larger proportions of Walrasian components in the assembly of their models. Applied general equilibrium researchers can no longer claim that macro modelling is orthogonal to their research interests and can therefore safely be ignored. This means that gradually the debate between macroeconomists and CGE modellers can be shifted to relatively minor aspects of the models. This is progress!

²⁶ See, for example, McKibbin and Siegloff (1988b), or Galeotti (1988).

²⁷ For example, empirical evidence for the Euler equations implied by life-cycle or permanent income consumption models is very weak.

²⁸ The specification used for investment in MM is an example: it attempts to have both good fit and sound underpinnings by using a lag structure in the short run while driving the long-run results by Tobin's q . The money demand equations used in both MM and MSG2 are another example because neither one is derived from optimization. It is, of course, possible to derive the demand for money as the solution to an explicit intertemporal optimization problem; see, e.g., Adams (1991).

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