



### National CGE Workshop 2016

Old Parliament House, Canberra Monday August 8, 2016



Abstracts and Presentations



National CGE Workshop 2016



Old Parliament House, Canberra Monday August 8, 2016

8:00	Open for Registrations	
8:30	Welcome and introduction	
Keynote	Speaker	
8:45	Mark Cully, Department of Industry, Innovation & Science	Modelling as <i>ex ante</i> policy evaluation
Session :	1: Chair Rod Tyers	
9:30	Rob Waschik, Centre of Policy Studies, VU	Linking CGE and specialist models: Deriving the implications of highway policy using USAGE-Hwy
10:00	Tim Murray, Productivity Commission	Integrating a Partial Equilibrium model within a CGE framework (as a Mixed Complementarity Problem)
10:30	Morning tea	
Session 2	2: Chair Philip Adams	
11:00	Cedric Hodges, Deloitte Access Economics	Are we there yet? Adjustment paths in response to Tariff shocks: a CGE Analysis.
11:30	<b>Bruce Layman</b> , Economic Regulation Authority of Western Australia	CGE Modelling in Python: an application to electricity market trading-interval dispatch
12:00	Peter Dixon, Centre of Policy Studies, VU	DSGE modelling in GEMPACK
12:30	Lunch	
Session 3	3: Chair Guy Jakeman	
13:30	Maureen Rimmer, Centre of Policy Studies, VU	Immigration reform scenarios for U.S. agriculture
14:00	Rod Tyers, UWA	Contractions in Chinese fertility and savings: long run domestic and global implications
14:30	Paul Gretton, Crawford School, ANU	Modelling the potential impacts of economic reform in a partnership between Australia and China
15:00	Afternoon tea	
Session	4: Chair Paul Gretton	
15:30	Xiao-guang Zhang, Productivity Commission	Solving a partial equilibrium model in a CGE framework: the case of a BMS model
16:00	Matt Clark, Synergies Economic Consulting	Economic benefits from reforms to management of the East Coast Trawl Fishery
16:30	Janine Dixon, Centre of Policy Studies, VU	The implications of a cut to company tax in Australia
17:00	Close	
	Workshop dinner: 6pm at Boffins R	estaurant, University House, ANU

This is an informal dinner at participants' own expense





### National CGE Workshop 2016

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Abstracts

#### Linking CGE and specialist models: Deriving the implications of highway policy using USAGE-Hwy

#### Peter B. Dixon, Maureen T. Rimmer and Robert Waschik

Scientists/engineers create specialist partial-equilibrium models of energy, environment and transportation. We show how technical information from such models can be transferred into a CGE model. We illustrate the approach by describing the creation and application of USAGE-Hwy which combines USAGE, a CGE model of the U.S., with HERS, a specialist highway model. USAGE-Hwy, translates micro information from HERS on the effects of highway expenditure programs into implications for GDP, employment, and the trade-off between current and future living standards. Combination models such as USAGE-Hwy bring scientific/engineering analyses into the economic domain, facilitating the use of these analyses in policy discussions.

## Integrating a Partial Equilibrium model within a CGE framework (as a Mixed Complementarity Problem)

#### Tim Murray

A number of different modelling frameworks have been used historically to address different policy questions. Partial equilibrium models have typically been used where engineering or industry-specific details are of particular importance; while CGE models have been used where economywide implications and inter-industry linkages are important. However, the two frameworks have a common mathematical and conceptual origin. Recent developments in approaches to designing and solving models presents an opportunity for incorporating typical PE characteristics (e.g. engineering characteristics) into detailed CGE models.

This presentation includes a proof of concept illustration integrating an energy model (which includes physical laws, as well as a nodal supply representation) within a CGE model (which includes typical CGE characteristics such as a number of industries, primary factors, taxes, as well as CET and CES relationships).

#### Are we there yet? Adjustment paths in response to Tariff shocks: a CGE Analysis.

#### Tony Wiskich and <u>Cedric Hodges</u>

This paper takes the mini USAGE model developed by Dixon and Rimmer (2005) and modifies it in order to better mimic the expected adjustment path following a tariff reduction. Results from the adjusted model are compared against the standard model. It is found that the standard model does a good job of capturing the expected long-run behaviour of the economy in response to this shock and, with a few relatively straight forward changes the standard model can retain the long-run outcomes and also have a more plausible adjustment path. These changes are documented in an appendix and are considered applicable to a wide range of models currently in use.

#### CGE Modelling in Python: an application to electricity market trading-interval dispatch

#### Bruce Layman

Python is an open-source, object-orientated interpreted programming language, while Pyomo is a Python optimisation modelling package that can be used to solve CGE models in the tradition of solving GTAP with GAMS software. This paper finds that while Python/Pyomo lacks the ease of use of GEMPACK for CGE modelling, its flexibility allows the implementation of assumptions different to standard CGE treatments. In particular it uses Python and Pyomo to construct: a simple stylised recursive-dynamic CGE model with forward-looking expectations in response to a known but staged policy change; and a simple stylised short-run comparative-static CGE model with an integrated electricity market trading-interval dispatch model. Its preliminary results indicate that forward-looking expectations lead to a more immediate investment response to a known staged policy change than comparative-static expectations, while the economic impact of increasing the supply of intermittent non-storable renewable energy production depends on how strongly this production correlates with electricity demand.

#### DSGE modelling in GEMPACK

#### Peter B. Dixon and Maureen T. Rimmer

This paper has two purposes. The first is to explain DSGE in a way that is comprehensible to CGE modellers with little experience in DSGE. The second is to show that DSGE models can be solved in GEMPACK. This is achieved by demonstrating a GEMPACK solution of the main illustrative model set out in Schmitt-Grohé and Uribe (2004). The GEMPACK approach offers the possibility of including DSGE features in full dimension CGE models.

#### Reference

Schmitt-Grohé, S. and M. Uribe (2004), "Solving dynamic general equilibrium models using a secondorder approximation to the policy function", Journal of Economic Dynamics and Control, vol 28, pp. 755-775.

#### Immigration reform scenarios for U.S. agriculture

#### Peter B. Dixon and Maureen T. Rimmer

The general equilibrium method adopted here reveals several effects of agriculture-focused immigration policies that would not have emerged in partial equilibrium analysis applied to agriculture. Our general equilibrium model includes specifications of: inter-sectoral labor flows; the role of vacancies in determining occupational choices; and macroeconomic relationships. This enables us to show that agricultural guest-worker and legalization programs are likely to: have similar effects on the agricultural sector; cause a gradual welfare-enhancing transformation of the occupational mix of incumbent employment away from agriculture; have small (possibly negative) effects on farm income; and have positive effects on aggregate capital, employment and GDP.

#### Contractions in Chinese fertility and savings: long run domestic and global implications

#### Rod Tyers

Following three decades of rapid but unbalanced economic growth, China's reform and policy agenda are set to rebalance the economy toward consumption while maintaining a rate of GDP growth near seven per cent. Among the headwinds it faces is a demographic contraction that brings

slower, and possibly negative, labour force growth and relatively rapid ageing. While the lower saving rates that result from consumption-oriented policies and rising aged dependency may contribute to a rebalancing of the economy, in the long run they will reduce both GDP growth and per capita income. Moreover, while an effective transition from the one-child policy to a two-child policy would help sustain growth and eventually mitigate the aged dependency problem, it would set real per capita income on a still lower path. These conundrums are examined using a global economic and demographic model, which embodies the main channels through which fertility and saving rates impact on economic performance. The results quantify the associated trade-offs and show that continuing demographic and saving contractions in China would alter the trajectory of the global economy as well.

#### Modelling the potential impacts of economic reform in a partnership between Australia and China

#### Paul Gretton

Effective economic reform agendas provide a means for promoting national economic growth, raising living standards and adapting to changes in trading conditions, new technologies and ways of working. Taking as a focus the Australia-China economic relationship, the GTAP model of the global economy is used to project the implications for Australia and China of preferential, unilateral and broader approaches to trade liberalisation, a broad agenda for reform across the services sector and financial market reform. The simulations show that reform strategies based on non-discriminatory trade liberalization and broadly-based concerted domestic reforms are likely to deliver substantive economic benefits and contribute to growth. Agendas that are restrictive, either through preferential deals between trading partners or through a narrow sectoral focus domestically are likely to constrain gains below levels that would otherwise be attainable.

#### Solving a partial equilibrium model in a CGE framework: the case of a BMS model

#### Xiao-Guang Zhang

This paper presents a new approach to decompose an integrated computable general equilibrium (CGE) model into a partial equilibrium (PE) model and a residual CGE model. This opens up the scope for richer analysis of policy relevant matters by expending the PE sub-model in selected circumstances.

Specifically, this paper outlines how to integrate a behavioural microsimulation (BMS) model within a CGE framework. It then shows how the household module can be separated from the CGE model and how the resulting PE sub-model and CGE model can be solved iteratively, so that the equilibrium is identical to that of the integrated model. The paper focuses on two challenges that arise when linking and solving two different models: how to find a convergent solution and how to ensure it is the true general equilibrium solution. This involves ensuring that databases and theory in both models are consistent and fit exactly with each other. Some cases may require the use of a slack variable to account for temporary inconsistencies between the two models.

This approach has the potential to extend the range and quality of the analysis of policy relevant issues. For example, using a microsimulation framework for the household sub-model, makes a richer analysis of the household sector transfer and tax system possible. Further work is required to investigate whether the general framework used for this specific partitioning of the structure of the model can be applied to structural partitions that relate to the other parts (eg the inter-industry part) of a CGE model.

#### Economic benefits from reforms to management of the East Coast Trawl Fishery

#### Matt Clark

The East Coast Trawl Fishery is Queensland's largest and most important commercial fishery. The fishery operates from the Gold Coast to Cape York and generates over \$90 million in gross value of production per annum. The fishery is currently managed through the effort units which grant fishers a perpetual right to fish for a regulated amount of time each year. This regulatory regime has created significant incentives for inefficiencies and effectively means the industry is regulated by economic conditions rather than an effective catch constraint.

Modelling has been conducted in MMRF to demonstrate how economic benefits might accrue from reforms to the fishery.

#### The implications of a cut to company tax in Australia

#### Janine Dixon and Jason Nassios

We investigate the impact of a cut to the company tax rate using a miniature version of the Vic-Uni computable general equilibrium model of the Australian economy with additional detail on ownership of physical capital. Because of Australia's system of dividend imputation, a change to the company tax rate disproportionately affects the final post-tax rate of return for foreign investors. Therefore a cut to the company tax rate would transfer government revenue to foreigners, and add to pressure on government to reduce spending or to raise personal taxes.

We find that a cut to the company tax rate would attract more foreign investment to Australia, making workers more productive and increasing wages and output. However, there is a lag between new investment activity and capital growth, and a large share of future company profits will accrue to foreign investors. We also find that increased wages will reduce returns to domestically owned capital.

While the impact on national *production*, as measured by GDP, will be positive, this is not a suitable measure of national benefit. The right indicator of national benefit is the impact of a company tax rate cut on national *income* and we find that this will fall.

### Linking CGE and specialist models: Deriving the implications of Highway Policy using USAGE-Hwy

8 August 2016

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#### Introduction: CGE models have been developed and used to address economic policy issues for many decades Reflect standard neoclassical utility maximization and costminimization problems, assuming CRS production in perfectly competitive markets But there is a large body of specialist theory and empirical information that can be brought to bear in a CGE framework Energy/environment modelling Water policy modelling Transport policy modelling Objective of this paper is to show how information from a specialist highway model, the Highway Economic Requirements System (HERS), can be transferred into a CGE model, USAGE, to deliver policy results that are informed by both modelling techniques VICTORIA UNIVERSITY MELBOURNE AUSTRALIA CoPS © copyright Centre of Policy Studies 2016 P.2



Creation o	f U	ISAG	E-H	wy:					
			Absor	ption Ma	trix				
	1	1	2	3	4	5			
		Prod-	Invest-	House-	Exports	Govt			
-		ucers	ors	holds					
	Size	$\leftarrow I \rightarrow$	$\leftarrow I \rightarrow$	$\leftarrow 1 \rightarrow$	$\leftarrow 1 \rightarrow$	$\leftarrow 1 \rightarrow$			
Basic Flows	$C \times S$	BAS1	BAS2	BAS3	BAS4	BAS5			
Margins C	↑ C×S×N ↓	MAR1	MAR2	MAR3	MAR4	MAR5			
Sales	↑								
Taxes	$\stackrel{C\times\!S}{\downarrow}$	TAX1	TAX2	TAX3	TAX4	TAX5			
Labour	$\stackrel{\uparrow}{\stackrel{M}{\rightarrow}}$	LAB0CCIND	C = I = 1	Number of Number of	commoditi	es $(62 \rightarrow (59 \rightarrow )$	68) 65)		
Capital	$ \begin{array}{c} \uparrow \\ 1 \\ \downarrow \end{array} $	CAPITAL	S = M = N = N	2; domestic Number of Number of	e and impor f occupation commoditi	ted 1s es used as 1	nargins		
Si	$J$ $ize$ $\uparrow$ $C$ $\downarrow$	foint Production Matrix ← I → MAKE		Size $\uparrow$ $C$ $\uparrow$ $\downarrow$	Import Duty $\leftarrow 1 \rightarrow$ TARIFF				
© copyright Centre of Policy Studies 2	2016						P.4	MELBOURNE AUSTRALIA	CoPS







Travel	time:							
<ul><li>Estimate linking tr</li><li>Introduce</li></ul>	travel tin avel time e a phan	me by e to vo tom ta	trans olume ax equ	sport t of tra ual to t	ype, and i vel/transp the labor o	ntroduce e port cost of trav	equati vel tim	ons e
		Value of travel time (\$ per hour)	Time lost (m. of hours)	Fraction of time lost deduced from labor supply	Deduction from labor supply (m. person years)	Phantom tax on sales (\$m)		
		(1)	(2)	(3)	(4)=(2)*(3)/2000	$(5) = (1)^*(2)$		
	Sales to VT							
	AirInternal	5	974	0.1	0.0487	\$4,870		
	PRT	5	13,448	0.1	0.6724	\$67,241		
	PassengTrans	5	5,910	0.1	0.2955	\$29,550		
	WaterInternal	0	0	0.0	0.0	0		
	Sales to CT							
	AirInternal	15	16	0.25	0.002	\$240		
	PRT	15	61,263	0.25	7.6579	\$918,945		
	PassengTrans	15	8,704	0.25	1.0881	\$130,568		
	WaterInternal	15	384	0.25	0.0479	\$5,753		
© copyright Centre of Po	licy Studies 2016					P.8		(CoPS)















































<b>2.</b> Generat	tion					
		Brown Coal	Black Coal	Gas Combined Cycle	Gas Open Cycle	Wind
Plant Availability	no.	0.97	0.97	0.99	0.99	0.25
Plant Size	MW	750.00	750.00	349.00	530.00	100.00
Fuel Cost	\$/GJ	0.40	2.25	7.00	7.00	0.00
Capital Cost	\$m/MW	4.39	2.88	1.09	0.73	2.56
Life of Plant	years	50.00	50.00	30.00	40.00	25.00
Thermal Efficiency		0.29	0.42	0.51	0.35	1.00
Carbon Emissions Capital Cost Equivalent Annual Value	tCO2e/MWh \$m/MW	1.13 0.37	0.74	0.35	0.52	0.00
Operational Cost	\$m/GW	0.0050	0.0195	0.0498	0.0728	0.0000
Productivity Cor	nmission					10



#### 2. Power System Economics 101 (cont'd) Transmission power flow



<b>3. Traditio</b> Input-C	onal CGE 10 Dutput core	1	
	Production activities	Final demands	Row Total
Goods	Inter-industry flows	Final demands	
Primary factors	Value added		Total income
Column total		Total expenditure	
Productivity Co	ommission		13























	Basecase	RenewableEnergy Target
n1	851	639
n2	-822	-812
n3		212
n1	850	473
n2	-781	-690
n3		238
n1	687	347
n2	-669	-577
n3	0	244
n1	548	202
n2	-537	-426
n3		232
n1	459	212
n2	-449	-342





## **6.** Nodal price at each end of the transmission link by load block and simulation (\$ per MWh)

_						
	Basecase	Basecase	Basecase	Renewable Energy Target	Renewable Energy Target	Renewable Energy Target
	n1	n2	n3	n1	n2	n3
b1	5648	7633		5649	8030	7775
b2	72	87		72	77	75
b3	58	62		58	61	59
b4	32	34		32	33	32
b5	8	9		5	5	5

6	• <i>Revenue, cost and profit for transmission line by simulation (\$m)</i>				
		Basecase	RenewableEnergy Target		
÷	Revenue	196668	168133		
	Annualised capital cost	196668	168133		
	Profit	0	0		
	Productivity Commi	ssion	29		

# **6.** End-user electricity prices by load block and simulation (\$ per MWh)

		[	
		Basecase	RenewableEnergy Target
b1	Electricity Market Price	7633	8030
b1	Renewable Energy Surcharge		15
b1	Total	7633	8044
b2	Electricity Market Price	87	77
b2	Renewable Energy Surcharge		15
b2	Total	87	92
b3	Electricity Market Price	62	61
b3	Renewable Energy Surcharge		15
b3	Total	62	76
b4	Electricity Market Price	34	33
b4	Renewable Energy Surcharge		15
b4	Total	34	48
b5	Electricity Market Price	8	5
b5	Renewable Energy Surcharge		15
b5	Total	8	19
Pr	oductivity Commission		30

## **6.** Price and quantity of fuel used for electricity generation (\$ per GJ and PJ)

			Basecase	Renewable Energy Target
Price	\$ per GJ	Primary Energy Brown Coal	0.4000	0.3713
		Primary Energy Black Coal	2.2500	2.2254
		Primary Energy Natural Gas	7.0000	7.0082
Quantity	PJ	Primary Energy Brown Coal	501	344
		Primary Energy Black Coal	33	24
		Primary Energy Natural Gas	50	51

Productivity Commission

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## **6.** Carbon emissions from power stations by simulation (Mt CO2e)

	Basecase	RenewableEnergy Target
Brown Coal	45.4	31.2
Black Coal	2.6	2.0
Gas Combined Cycle	2.2	2.2
Gas Open Cycle	0.2	0.3
Total	50.5	35.6

**Productivity Commission** 

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	Basecase	RenewableEnergy Target
CPI	100.00	100.24
Nominal Wage	80.50	80.30
Real Wage	80.50	80.11

# **6.** Employment of labour in production of goods and services (core CGE)

	Basecase	RenewableEnergy Target
Agriculture	41.63	41.59
Mining	24.23	24.16
Manufacture	190.24	189.84
ElecRetailDistn	1.23	1.21
GasRetailDistn	0.30	0.30
Services	1376.95	1376.70
BrownCoalProd	0.28	0.17
BlackCoalProd	8.66	8.61
GasProd	2.56	2.57

**Productivity Commission** 

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### 6. Price of domestic production

	Basecase	Renewable Energy Targel
Agriculture	200.00	200.01
Mining	200.00	200.15
Manufacture	200.00	200.23
GasRetailDistn	200.00	200.14
Services	200.00	200.06
BlackCoalProd	2.25	2.25
GasProd	7.00	7.00

Productivity Commission

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#### Quantity of export goods 6. Renewable Basecase Energy Target 19.70 19.69 Agriculture Mining 32.65 32.53 Manufacture 56.86 56.53 GasRetailDistn 0.31 0.31 Services 140.06 139.86 BlackCoalProd 2543.38 2535.40 GasProd 135.82 135.57

Productivity Commission

### 6. Quantity of composite final goods

	Basecase	Renewable Energy Target
Agriculture	50.12	49.99
Mining	73.00	72.70
Manufacture	566.28	564.63
ElecRetailDistn	32.98	32.37
GasRetailDistn	3.13	3.12
Services	1628.24	1625.86
BrownCoalProd	500.96	343.92
BlackCoalProd	179.69	170.99
GasProd	329.79	330.26

Productivity Commission

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	Real change \$m					
Consumption	-652					
Investment	10					
Government	0					
Exports	-149					
Imports	-94					
6	. Macro re	sults –	Welfar	re		
---	-------------------------	-------------------------------	--------------------------------	----------------------	----------------	-------------
		Marginal Utility Income	Nominal Household Income	Household Utility	Nominal GDP	Real GDP
	Change	-0.002	-323	-650	-295	-696
	Productivity Commission				39	



## Are we there yet? Adjustment paths in response to Tariff shocks: a CGE Analysis

Tony Wiskich and Cedric Hodges



- Motivation
- The original model
- Adjustments
- The adjusted model
- Conclusion

# Motivation

- What is the problem we are trying to solve?
- What have we done to address it?
- Why have we done it this way?

## The Original Model

- We have used miniature version of the US AGE model (mini-USAGE) developed by Dixon and Rimmer (2005).
  - Same as big-USAGE in terms of theoretical structure but run with a more aggregated database.
  - 2 regions (US, RoW), 5 sectors (low/high protection, construction, services, government) and 2 factors (labour, capital).

# The Original Model

- We shock the tariff rate on highly protected goods down by 5 percentage points (from 10% to 5%) permanently in the first year of 10 year simulation.
- This is offset by changes in the labour income tax rate (a standard closure).
- There are no other shocks.



















# Adjustments

- Three more adjustments:
  - We introduce a price level variable, giving us a degree of freedom.
  - We use this degree of freedom to set the real exchange rate consistent with forward looking interest parity.
  - We introduce a central bank who follows a Taylor rule.

Original	Real	Nominal
No changes	Time varying export elasticities	Time varying export elasticities
	Current account consumption link	Current account consumption link
	Capacity utilisation	Capacity utilisation
	Phillips curve	Phillips curve
		Price level variable
		Forward looking interest parity
		Taylor rule



























Interest parity and Taylor rule  

$$\frac{e}{e} = \frac{1+0.5*(R_{\odot}+R}{1+R}$$

$$= -1$$

$$R_{\odot} = (=5+)+0.5(L_{\odot}-L)$$

$$\pi_{\odot} = -\pi \quad \Leftrightarrow \odot$$

# Using Python/Pyomo to Undertake CGE Modelling: An Application to Forward-looking Expectations and Electricity Market Policy Changes

Bruce Layman

Chief Economist

Economic Regulation Authority of Western Australia\*

#### Abstract

Python is an open-source, object-orientated interpreted programming language, while Pyomo is a Python optimisation modelling package that can be used to solve Computable General Equilibrium (CGE) models in the tradition of solving GTAP with GAMS software. This paper finds that while Python/Pyomo lacks the ease of use of GEMPACK for CGE modelling, its flexibility allows the implementation of assumptions different to standard CGE treatments. In particular it uses Python and Pyomo to construct: a simple stylised recursive-dynamic CGE model with forward-looking expectations in response to a known but staged policy change; and a simple stylised short-run comparative-static CGE model with an integrated electricity market trading-interval dispatch model. Its preliminary results indicate that forward-looking expectations lead to a more immediate investment response to a known staged policy change than comparative-static expectations, while the economic impact of increasing the supply of intermittent non-storable renewable energy production depends on how strongly this production correlates with electricity demand.

\*The views presented herein are those of the author and should not be taken as reflecting the views of the Authority, individual members of the Authority, the Authority's Secretariat, or members of other organisations. The Author acknowledges the time and support from the Authority to undertake this paper.

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## Introduction

Since its introduction in 1984, GEMPACK (Horridge and Pearson, 2011) has facilitated some of Australia's most influential policy advice through the Centre of Policy Studies (CoPS) suite of models. It is also used in over 400 other locations in 60 countries. This is likely to continue in the future and for good reason.

GEMPACK allows modellers to solve large systems of simultaneous equations and, once some basic intuitive GEMPACK coding language is learned, it frees modellers to concentrate on the economics of a problem without worrying about computational issues or onerous data input and output considerations.

Additionally, the CoPS suite of models from ORANI (Horridge, 2014) to the Victoria University Regional Model (VURM, formerly MMRF, Peter, Horridge, Meagher, Naqvi and Parmenter, 1996) has allowed researcher to ask policy questions, perhaps with some slight modifications to the base model, without having to construct a Computable General Equilibrium (CGE) model and database from scratch. The author has used MMRF in particular to analyse a number of policy questions related to the Western Australian economy.

This study is conducted to undertake the somewhat eccentric task of CGE modelling outside of the CoPS/GEMPACK paradigm, although the basis for the modelling is firmly rooted in the CoPS linearised CGE tradition.

It is motivated by a desire to test the Python programming language and its Pyomo package, which can already be used across a range of uses, to another purpose. The attraction of a language with a wide range of uses is that, even if it is not the best for any single purpose, it potentially enables researchers to learn how to use only one language to undertake a range of tasks. This reduces the fixed cost of learning the background language for each task.

Another potential benefit from using Python for CGE modelling is that there is flexibility to go beyond the boundaries of GEMPACK's limits, although this increased flexibility comes with increased risk of model failure and data handling errors. Hence this study attempts to solve CGE models in ways that in the author's knowledge have not been used before.

This paper constructs simple stylised models to illustrate: a recursive dynamic model with forward looking expectations to deal with a policy change that is phased in over time; and a comparative-static model that is directly integrated with an electricity market dispatch model in the same Python file.

Both of these simulations are based on stylised or toy models with fictitious databases. This paper does not claim that the results hold beyond the models presented, either in terms of Python/Pyomo solving large scale CGE models or that the results presented have any practical policy implications. They do, however, suggest that further research in these areas could be useful.

This paper has been prepared by Bruce Layman, Chief Economist, in the Economic Regulation Authority (ERA) of Western Australia Secretariat. The views presented herein are those of the author and should not be taken as reflecting the views of the Authority, individual members of the Authority, the Authority's Secretariat, or members of other organisations.

## Python/Pyomo

#### Python

#### Description

Python (Chan, 2014) is a general-purpose interpreted, interactive, object-oriented, and high-level programming language.<sup>1</sup> It has been used for many different software products and applications in the field of science and finance.<sup>2</sup>

Python is open source, meaning that it is free to use, even for commercial applications. It is managed by the Python Software Foundation<sup>3</sup>. However, there are commercial products leveraged off Python, while additional commercial software is sometimes required to run Python packages.

It is an object-orientated programming language, meaning that it focuses on the data or objects being analysed, rather than on the logic required to manipulate them as in procedural languages. Fortran, on which GEMPACK is based (Horridge and Pearson, 2011), is a procedural language.

It is an interpreted language, meaning its instructions are implemented directly rather than having to compile functions into machine-language instructions. This means that the program is slower to run, but allows the code to be more intuitive than for a compiled language. This is increasingly an advantage in a world where computer processing power is increasing and becoming cheaper every year.

Python is run on a text editor or inside an 'Integrated Development Environment' (IDE), which provides additional facilities for programmers. There are many popular Python IDEs. The calculations in this paper were constructed in the Anaconda<sup>4</sup> environment, which has many mathematical and scientific packages preinstalled.

Python may be run interactively in an IDE, or saved as a Python (.py) file, from which large blocks of code can be run.

Python has a large number of additional 'packages' that can be installed and called in a Python script. Such packages are sometimes difficult to install, but allow users to call intuitive functions to perform common and many less common tasks. Consequently, users do not need to be programmers with an extensive knowledge of Python programming concepts, but simply informed users of the packages that can be called to perform complex data manipulation tasks.

Python packages must be explicitly imported into Python scripts for which they are needed. For example, to call the 'pandas' package, which organises large datasets into dataframes (an organised spreadsheet-like table), the following Python script is run:

<sup>&</sup>lt;sup>1</sup> Python for Unix/C Programmers Copyright 1993 Guido van Rossum 1 (1993), <u>http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.38.2023</u>.

<sup>&</sup>lt;sup>2</sup> A list of companies that use Python and products written with Python is available at: <u>http://brochure.getpython.info/media/releases/psf-python-brochure-vol.-i-final-download.pdf/view</u>.

<sup>&</sup>lt;sup>3</sup> Information on the Python software Foundation can be found at: <u>https://www.python.org/psf/</u>.

<sup>&</sup>lt;sup>4</sup> Details of the Anaconda Environment can be found at: <u>https://www.continuum.io/downloads</u> .

#### import pandas as pd

If the user requires a new dataframe using simple data directly inputted their keyboard, the following command could be used:

 $df = pd.DataFrame(\{ a': [1,2,3], b': [2,3,4] \}).$ 

The 'pd' is required to call the package, while 'DataFrame' is a function from within the package. This creates the following dataframe:

	а	b
0	1	2
1	2	3
2	3	4

The data are contained in columns 'a' and 'b', which the leftmost column of cells is the (yet unnamed) index.

In reality, base input data are more likely to be imported from spreadsheets, csv files or database products such as SQL. For example, it is straightforward for Python scripts to access information in a SQL database using the 'pymssql' package. This package executes SQL code written inside the Python script to access the SQL data.

As Python is open source, there are many discussion boards and websites dedicated to Python education and answering programmer questions. In all likelihood, if a user has a problem, some else has solved it and posted it online.

For example, the popular 'Stack Overflow' question and answer website for programmers<sup>5</sup> has over 600,000 questions directly tagged as 'Python', as well as many tens of thousands of questions each dedicated to individual Python topics.

#### Data Manipulation Example

As an example of data manipulation in Python, the following code retrieves 2015 Western Australian Wholesale Electricity Market (WEM) data of the Australian Energy Market Operator (AEMO) website, creates a dataframe containing only trading interval-by-trading interval system demand in Megawatts (MW)<sup>6</sup>, and then charts this information.

import pandas as pd

import matplotlib.pyplot as plt

url =http://data.wa.aemo.com.au/datafiles/balancing-summary/balancing-summary-2015.csv

 $table = pd.read_csv(url)$ 

df1=pd.DataFrame(table)

<sup>&</sup>lt;sup>5</sup> This can be found at: <u>http://stackoverflow.com/</u>. The data are current as at 1 August 2016.

<sup>&</sup>lt;sup>6</sup> Megawatts (MW) are units of power. Megawatt hours (MWh) are a measure of energy, or work multiplied by time.

df2=pd.DataFrame(df1['Scheduled Generation (MW)']) df2.columns=['MW'] plt.plot(df2['MW']) plt.title("Figure 1: WEM Demand (MW)", size=18) plt.ylim(1000, 4000)

This generates Figure 1 below.



However, if the user were interested in the WEM's load duration curve, with demand ordered from the highest quantity to the lowest quality<sup>7</sup>, they could create a new dataframe and reorder these data. Alternatively, if they wished to view the reordered data in a chart but leave the df2 dataframe untouched, and add a chart title and axes labels, the following plot command could be used:

plt.plot(df2.sort(['MW'], ascending=[False]))

plt.title("WEM Load Duration Curve (MW)", size=18)

plt.xlabel('Trading Interval', fontsize=12)

<sup>&</sup>lt;sup>7</sup> Examining load duration curves are useful for power system or individual generator planning purposes.

plt.ylabel('MW', fontsize=12)

This code creates Figure 2 below.



#### Pyomo

#### Summary

Python Optimising Modelling Objects (Pyomo, Hart, Laird, Watson and Woodruff, 2012) is a Python package that 'supports the formulation and analysis of complex optimisation applications'. A simple optimisation problem is described in the next section.

While Python is an object-orientated language<sup>8</sup> and Fortran is a procedural language, in practice there is very little difference to a modeller in terms of how GEMPACK and Pyomo operate. The type of model used in the main simulations in this paper is an abstract model, which means that the code constructed can be used on different datasets.

Sets, parameters and variables have a similar meaning to the same terms in GEMPACK. Constraints are Pyomo optimisation functions that play a similar role as GEMPACK Equations. Constraints are further explained in the next section. Calculating initial

<sup>&</sup>lt;sup>8</sup> In object-orientated programming terms, the Pyomo model type 'AbstractModel' is a Python class and a model constructed with that code is an instance of that class. Hence the term 'model= AbstractModel()' is included in the code near the beginning of the script, and all variables, the objective function and constraints are defined in terms of that instance. For example, in Pyomo a variable 'X" is defined as 'model.X'.

parameters, as is done with formulas in GEMPACK, is done with Parameter Initialisations in Pyomo.

As an example of Pyomo versus GEMPACK code, consider the standard equation for industry demand for labour taken from the Mini-USAGE model (Dixon and Rimmer, 2005). In GEMPACK the equation is:

Equation E\_x1lab # Industry demands for labour # (All,i,IND) x1lab(i) - a1lab(i) = x1prim(i) - SIGMA1PRIM(i) \* [p1lab(i) - p1prim(i)];

In contrast, the Pyomo Constraint is as follows:

def E\_x1lab (model,i):
return model.x1lab[i] == model.x1prim[i] model.SIGMA1PRIM[i]\*(model.p1lab[i]-model.p1prim[i])
model. E\_x1lab = Constraint(model.IND, rule= E\_x1lab)

While there are differences in Syntax, the basic structure of the relationship is clear in both expressions.

Pyomo requires an optimisation solver program to run. The solver's required capabilities, such as linear versus no-linear programming or whether it supports mixed-integer programming or not, depends on the problem to be solved. Solvers range from free open source programs to very expensive commercial applications.

The models in this paper solve quickly using both the free CBC solver<sup>9</sup> and the commercial CPLEX<sup>10</sup> solver, but the models slow dramatically once additional complexity is included in the models. This is especially the case for the electricity dispatch model described later, which slows dramatically on both solvers once additional constraints are included.

## **Mathematical Optimisation Techniques**

#### Linear Programming

#### **Basics**

Optimisation modelling seeks to solve for an 'objective function' relative to a set of constraints. For example, the models in this paper use a subset of optimisation modelling in Linear Programming (LP).

Briefly, LP is an optimisation procedure for linear objectives and constraints. Formally, for a vector of variables of interest x, vectors of parameters C and b and a matric of parameters A, an LP problem can be specified as:

<sup>&</sup>lt;sup>9</sup> For more information on the CBC solver see: <u>https://projects.coin-or.org/Cbc</u> .

<sup>&</sup>lt;sup>10</sup> For more information on the CPLEX solver see: <u>https://www-01.ibm.com/software/commerce/optimization/cplex-optimizer/</u>.

Maximise $C^T x$ Subject to:Ax <= b

x>= 0

 $C^{T}x$  is the objective function, while  $Ax \le b$  are the model constraints. The remaining terms sets the lower bound for the solution.

To illustrate the LP problem, consider a simple example for two variables x1 and x2, with the parameters set to their numerical values:

Maximize: model.x1 + 2\*model.x2 Subject to:  $x1*3 + x2*4 \le 6$  $x1*2 + x2*7 \le 10$  $x1, x2=> 0^{11}$ 

This problem is shown graphically in Figure 3 below. The shaded area is the area below both constraint lines and, given both constraint inequalities are less-than-or-equal-to, is the area for which a solution is feasible. The optimal solution in this case is the intersection of the two curves in 0.15384615 for x1 and 1.3846154 for x2.



<sup>&</sup>lt;sup>11</sup> The solution for this problem is 0.15384615 for C1 and 1.3846154 for C2.

#### Practical Linear Programming Example

For a more practical example of linear programming, such models are often used to solve electricity market dispatch problems for a central planner or a market with centralised dispatch. Dispatch quantities from each generator in each time interval (variables) are optimised to minimise the total generation cost for the period of interest (the objective), given a known set of generators with known marginal costs and fixed total demand (parameters). This is a short-run process that minimises variable costs.

Figure 4 below shows the cost of electricity for a system as the power production increases. It is a step function, with the cheapest generator able to produce at \$30/MWh until it reaches its maximum level of production of 100 MW, before the next cheapest generator produces at \$35/MW for the next 100 MW, and so on.

If demand is initially 475 MW, the marginal generator's cost is \$55/MWh. If the system were a market, this generator would set the market price. To the left of 475 MW, generator constraints are binding because generators cannot exceed their maximum levels of production. To the right of 475 MW however, higher cost generators are not needed and so the constraints are not binding.



The natural way to solve this type of problem of cost minimisation is by LP. The non-binding constraints are solvable because generators can produce less than or equal to their maximum production, rather than only at a set level of production.

While the example explained above is trivial, real-world electricity market problems are not. For example, if demand fell to 300 MW as in Figure 5 below, a different set of constraints become binding.



Additionally, successive trading interval cost minimisation problems are not independent because:

- Generators also have minimum production levels, meaning that plants might be shutdown even though notionally there is some demand for their output;
- Generators cost (often substantial amounts) of money to start up and shut down, meaning they may keep running even though the market price is less than their marginal cost, or may not start up if they are needed for only a few trading intervals;
- Technical requirements of each generator may mean that they have a minimum number of trading intervals that they must be run for and a minimum number of trading intervals for which they must be rested once shutdown. These are called minimum-up and minimum down times; and
- Plants have technically safe minimum changes in output over time, or ramp rates.

Finally, the short-run marginal cost of many traditional electricity generators actually slope downwards, as they become more efficient as they move from their minimum generation level to their maximum generation. Consequently, over small changes in demand, costs can go up when demand falls.

These factors mean that, rather than a succession of independent cost minimisation problems, electricity dispatch over a time period is one single problem. <sup>12</sup> The overall time period may be divided up into multiple time periods, but care needs to be taken that initial and terminal conditions for each sub-period do not lead to unrealistic results<sup>13</sup>.

<sup>&</sup>lt;sup>12</sup> This model can be solved by the Mixed-Integer Linear Programming (MILP) technique, which allows binary variables. This is explained later in the electricity dispatch model details.

<sup>&</sup>lt;sup>13</sup> These can occur in situations where dispatch during trading intervals outside of the sub-sample affects dispatch inside the sub-sample. For example, it might make sense to shut-down a generator towards the end of a sub-sample if only the sub-sample was considered, but it might not make sense if this generator were required to be dispatched early in the next sub-sample.

#### **CGE Modelling using LP Techniques**

CGE modelling using optimisation techniques has been successfully conducted through the GAMS optimisation or the MPSGE GAMS subsystem software (Horridge and Pearson, 2011). GAMS has usually been used to solve nonlinear CGE problems such as those in various versions of GTAP (GTAP in GAMS, Rutherford, 2006)

The method used for GAMS is to set the objective function to zero and specify all the constraints as equalities rather than inequalities (Horridge and Pearson, 2011). This is in contrast to GEMPACK which solves an exactly identified set of linear equations.

As an example, consider the previous simple linear programming example. If the constraints are specified as equalities and the objective function is replaced with zero, the problem becomes:

Maximize:	0
Subject to:	x1*3 + x2*4 == 6
	x1*2 + x2*7 == 10
	x1, x2=> 0 <sup>14</sup>

In this case the solution to the problem is exactly the same as the LP optimisation above. However, rather than this solution being the maximisation within a feasible region, in a CGE model is the only possible solution.

<sup>&</sup>lt;sup>14</sup> The solution for this problem is 0.15384615 for C1 and 1.3846154 for C2.



The ability for Pyomo to solve system of equations that is not exactly identified can lead to difficulty in determining whether a CGE model has a valid closure. If the variable count is 1-2 variables over or under-identified, the model will still solve but will not give the 'correct' result. More than 1-2 variables from identification will lead to trivial solutions such as all price changes being equal to zero, and at some point the model will not solve.

## **Application 1: A Simple Dynamic CGE**

#### Model description

To illustrate the concept of forward looking expectations in a CGE model, a simple stylised model is created. The model has the following characteristics:

- It has linearised economic relationships;
- It has one good and one industry;
- It has labour and capital inputs, but no intermediate demands;
- It has one single price for the good, which is the model numeraire. This is discussed further below;
- It has an instantaneous short-run labour market closure;
- It has linearised CES production technology for labour and capital inputs;

- It has no margins, taxes or government expenditure;
- It is a closed economy with no exports or imports. Income in each year is spent on either consumption or investment with no net debt created; and
- It has a standard recursive-dynamic modification, specifically modelled on mini-USAGE model (Dixon and Rimmer, 2005)

The model is calibrated so that it is in a long-term steady-state, with investment in each year exactly equal to depreciation in the database. This removes the need to do separate base and base-rerun simulations, as the alternative to the policy simulation results is zero.

Unlike a model with an export/import module with an associated exchange rate, a simple closed-economy model does not specifically require the creation of an exogenous model price numeraire. However, a numeraire is used in this model as it facilitates the model's steady state.

If the single price in this model is specified as an exogenous numeraire, the model's consumption function is not required as the model's commodity market clearing constraint is equivalent to a nominal income constraint. This reduces the number of equations by one, which accommodates the additional exogenous variable.

#### **Dynamic CGE Modelling and Expectations**

Almost all dynamic modelling in the CoPs family of CGE modelling has been of the form of recursive-dynamic modelling, where a succession of comparative-static simulations are run with linking equations for stocks of capital and the database for each year is affected by the updated database from the previous year.

Dixon, Pearson, Picton and Rimmer (2003) note that recursive dynamic modelling has advantages over a fully specified dynamic modelling, where all years are solved simultaneously, as: the ability to solve larger and more detailed models with recursive-dynamic modelling; and higher transparency to the reader. With regard to the second point, even a percentage change model becomes non-linear under a simultaneous model, as the usual model coefficients become variables of the model rather than as input parameters.

Dixon et al (2003) note that the Monash Model static expectations formula is given by:

$$EROR(i,t)^{1} = EROR\_SE(i,t)^{1}$$

Dixon and Rimmer (2005) show that in practical terms, the static expectations rate of return calculation is given by:

$$100 * del\_ror = \left[ \left( \frac{1}{1 + RINT} \right) * \left[ \frac{V1CAP(i)}{VCAP(i)} \right] * (p1cap(i) - p2tot(i)) \right]$$

Where:

EROR(i,t) is the rate of return used in the model for industry I in year t;

EROR\_SE(i,t) is the static rate of return for industry I in year t. It is equal to 100\*del\_ror(i) in mini-USAGE;

del\_ror is the linear change in the rate of return for industry I;

RINT is the real interest rate;

V1CAP(i) are the gross returns to capital for industry i

VCAP(i) is the value of the capital stock in industry I;

p1cap(i) is the price of capital for industry I; and

p2tot(i) is the price of investment goods to industry 1.

The interpretation of the static returns expectations relationship is that the rate of return considered by investors in year t is the rate of return for year t discounted by one year to reflect the fact that returns from investments in year t will not be received until year t+1.

However, almost all capital created in year t+1 will have a life beyond that year. For example, if the same gross return was received in year t+2 as in t and t+1, it would need to be discounted by the real interest rate twice. Additionally, depreciation from year t+2 onwards would mean that the return would be on successively lower capital unless offsetting capital expenditure was made<sup>15</sup>.

Dixon et al. (2003) proposed a method to incorporate rational expectations into recursive dynamic models by iteratively ensuring that expected rate of return in each industry in year t is equal to the actual rate of return in year t+1, plus the residual value of the new capital at the end of year t+1.

Dixon et al. (2003) replace static expectations with one-year forward looking expectations, which they define as 'rational expectations'.

$$EROR(j,t)^2 = ROR\_ACT(j,t)^2$$

In this equation ROR\_ACT is the actual return plus residual value of the capital in year t+1.

$$ROR\_ACT(j,t) = -1 + \left[\frac{1}{1+INT}\right] * \left[\frac{Q(j,t+1)}{PI(j,t)}\right] + \left[\frac{1-D(j)}{1+INT}\right] * \left[\frac{PI(j,t+1)}{PI(j,t)}\right]$$

Firstly, the model is run under static expectations. Then the rate of return in year t is replaced by ROR\_ACT(i,t) (the actual return in year t+1) and the model runs again. If investment in year t changes relative to the initial comparative-static simulation, ROR\_ACT(i,t) will also change. As such it is required to loop the model until:

$$EROR(j,t)^{N} = ROR\_ACT(j,t)^{N}$$

The Dixon et al. (2003) method assumes that the residual value of new capital at the end of year t+1 is reflects only the change in the price of investment between year t and year t+1. Hence the investment is reversible at the end of period t+1. This might be a reasonable expectation for many or most industries, but it might not be appropriate for a specific class of policy shocks where the change is phased in over time and there is reasonable certainty of the path of the change.

Consider an import tariff change or the imposition of a carbon tax that a government announces is to be phased in over time. For example, a government might think that the social cost of carbon is \$100/t CO2, but that immediate imposition of such a tax would cause

<sup>&</sup>lt;sup>15</sup> The rate of return flows directly through to capital growth, not investment.

major costs on the economy. It therefore decides to start the tax at \$20/t in year one, rising by \$5/t per annum until it reaches \$100/t in year 16.

Under static expectations, investors will make decisions about their capital stock in year t+1 onwards based on a carbon tax of \$20/t, while under the Dixon et al method rational expectations method, they will consider \$25/t plus residual value at the end of year t+1.

Both of these methods are likely to understate the impact on investment decisions on (say) a coal-fired power station with an effective life of at least 30 years. Assuming a tax of \$20-\$25/t in an investment calculation is clearly too low for the life of the asset, while returns from year t+2 onwards are likely to be less than the cost-based residual asset value at the end of year t+1. This could have major implications for the pattern of investment in a CGE model policy shock.

Additionally, economic cost of such action on carbon will depend critically on a race between the investment impact of the increase in the carbon tax and the improvements in the cost and practicality of low-carbon technologies. CGE models are likely to underestimate the economic cost of a phased-in carbon tax if their investment responses lag those likely to occur.

This paper uses a similar method to Dixon et al (2003) to calculate the rate of return on an investment from year t until the terminal year of the analysis. This formulation is designed to be comparable to static expectations, except that it allows for deviations in the present value of returns from year t+1 to the terminal year. There is only one industry in the model, so the formula is:

$$\operatorname{ROR}_{\operatorname{ACT}}(t) = \left[ \left( \frac{1}{1 + RINT} \right) * \frac{V1CAP(t)}{VCAP(t)} * \frac{\left[ \sum_{u=t+1}^{T} (Q(u))^{u} \right]}{(T - (t+1))} \right]$$

The variables in this equation are the same as above. For example, if the static expectations rate of return increases from 5% in year t+1 to 6% in year t+2, EROR\_ACT(t) would be 5.5% discounted back from year t+1 to year t.

Neither the Dixon el al. (2003) method nor the method suggested in this paper is true rational expectations in terms of maximising consumption over time. Investment is based on an annual approximation the response of investment to changes in rates of returns. True rational expectations require moving to a single solution nonlinear model.

Additionally, the formula is greatly simplified by the adoption of only a single price in the model which is treated as an exogenous numeraire. This means that the formula does not have to account for changing investment prices.

Finally, the formula does not at this stage include a residual asset value for capital remaining at the end of the terminal year of the simulation. This could be improved in any future iterations of this method. Otherwise, the model could simply be run for a number of years after the period of interest ends, so that the present value of capital created during the period of interest is mostly depreciated.

The process to iterate expected and actual returns is as follows:

- 1. The model is run with static expectations, where EROR(t) = EROR\_SE(t)
- The actual rate of return for each year t to the terminal year is calculated as above (EROR\_ACT(t)<sup>0</sup>).

- 3. A vector of coefficients, DIFF, is created. This is the difference between the imposed expected rate of return in the model, versus the actual return once the model is run with investment based on these expectations.
- 4. A variable, tolerance, is created. This is the modeller accepted maximum error
- 5. The model is looped using the Python 'while' function as follows.

While DIFF(t) > tolerance(t):

Run model with EROR(t) = EROR\_ACT(t)<sup>1</sup>

Calculate EROR\_ACT(t)<sup>2</sup>

 $DIFF = abs(EROR\_ACT(t)^{1} - EROR\_ACT(t)^{2})$ 

 $EROR\_ACT(t)^1 = EROR\_ACT(t)^2$ 

If the absolute value of DIFF(t) is less than the tolerance, then the process ends. If the absolute value of DIFF(t) is greater than or equal to the tolerance, the model replaces  $EROR\_ACT(t)^1$  with  $EROR\_ACT(t)^2$  and starts the process again.

For the small model examined convergence is achieved relatively quickly (less 5 seconds) for a relatively small number of iterations (2-3 loops), negating the need for a partial adjustment mechanism to avoid result cycling (as described in Dixon et al., 2003). This paper does not examine whether this result holds for larger models.

#### **Policy Shock and Results**

A 2.5% per annum labour saving technology is applied to the model in the form of a shock to an exogenous variable in the model's labour demand equations.

As expected, the expected rate of return in the comparative-static simulation climbs gradually over time as the effect of the annual shocks compounds through the database. The forward-looking returns, however, are much larger at the start of the period as investors foresee the impact of the change on their returns from investment now in future years. This is shown in Figure 7 below.



Consistent with higher changes in rates of return in the early years of the model run, changes in investment starts much higher in the forward-looking expectation simulation that the comparative-static simulation and stays higher for the entire period. This is partially because investment early in the period causes the capital stock to grow rapidly, requiring greater investment to offset depreciation later. Investment for both simulations is shown in Figure 8 below.



The capital stock in year 9 rises very slightly under the forward looking expectations scenario, from \$1,016.1 million to \$1,017.4 million or 0.13% higher. The growth in capital from the steady state capital stock of \$1,000 million was 7.94% higher under forward looking expectations than under static expectations.

Figure 9 shows that real consumption in the forward-looking expectations simulation falls dramatically as the economy devotes more resources to investment rather than consumption in a closed system. In the later years of the forward-looking expectations simulation, consumption rises dramatically as the larger capital stock generates incomes and rates of return fall.



As noted above, the model does not optimise consumption over time, so the results are dependent upon how well the approximation of the dynamic investment response accurately represents the actual response in the economy. This is not an ideal situation, but solving to optimise consumption would entail solving a complex large non-linear model for all years considered simultaneously.

# Application 2: An Integrated CGE Model and a Detailed Electricity Generation Model

#### Background

The concept of combining the advantages of CGE models and electricity dispatch/market models is not new. For example in 2011 the MMRF CGE model and ROAM Consulting/SKA MMA electricity-sector models<sup>16</sup> were combined for Treasury's modelling of the Carbon Pollution Reduction Scheme (Treasury, 2011).

This process is described in Adams, Parmenter and Verikios (2016), where MMRF was combined with Frontier Economics' WHIRLYGIG model (Frontier Economics, 2009). The modelling process was:

- MMRF Provides information on fuel prices and other electricity-sector costs and on electricity demand;
- Given these assumptions, WHIRLYGIG generates detailed cost estimates for various generation types, which are then fed back into MMRF; and
- Information is passed back and forth between the models in a series of iterations until the retail price of electricity has stabilised in both models.

Adams et al. (2016) do not specify whether WHIRLYGIG is run with electricity demand specified in actual trading interval order (as in Figure 1 above) or as a load duration curve (Figure 2 above).

They note that using electricity market models has the advantage of increasing the technical detail, better simulate changes in generation capacity and increase in the policy detail that can be analysed.

Given the level of detail in each model, it makes sense to utilise the pre-existing detail in established model which has been built up over a many years, rather than start again with an integrated model.

Nevertheless, with improvements in computer processing power and the importance of the policy, this might not be the case indefinitely. This paper undertakes the first steps towards an integrated model, by linking still separate models communicating in a similar way to Adams et al. (2016), but combined in the same software file and with the looping process automated.

<sup>&</sup>lt;sup>16</sup> And other industry specific models.
#### The Models

#### CGE Model

The CGE model used in this simulation is a very simple. It is a linearised comparative-static model set to a short-run closure, with capital in each industry fixed and wages set to an economy-wide fixed level.

It is a three industry, three good model. The industries are electricity generation, resources (which supplies fuel to electricity generation) and services. The database for the model is simulated but the electricity sector is approximately scaled to that in the electricity dispatch model below. All industries are then scaled to the equivalent to the equivalent industries in the Australian Input-Output Table Direct Requirements Coefficients (Australian Bureau of Statistics, 2016).

The model has Leontief technology at the top level for intermediate inputs and primary factors. There is linearised CES substitution between primary factors. The model is a closed economy with no investment in which all outputs are consumed.

The model contains both a nominal income constraint and a commodity market clearing constraint, so has no general price numeraire as discussed above. The only fixed price is the economy-wide wage.

#### Electricity Markey Model

The electricity dispatch model used in this simulation is a straightforward standard but simplified model of electricity generator dispatch (modelled on a simplified version of Morales-Espańa, Latorre and Ramos, 2013). It is a Mixed-Integer Linear Program (MILP) in levels, which allows for binary variables to impose minimum generation constraints. In this model:

- There are 335 trading intervals, or approximately one week's worth of half hour trading intervals. Cost is minimised for a fixed level of varying demand across the entire 335 intervals;
- Demand varies between 876 MW (or 438 MWh per trading interval) and 2,456 MW per trading interval, and varies by trading interval according to daily fluctuations in winter demand in the Western Australian Wholesale Electricity Market (WEM). This is shown in Figure 10 below;



- It is energy-only dispatch, with no specific allowance for capital costs, as occurs in the National Electricity Market (NEM);
- There is a fixed capacity of generators of 3,150 MW. Generators have constant marginal costs of production between minimum and maximum generation levels;
- A generator can be shut down, but if it is to be dispatched it must be at no less than its minimum generation level. For example, a generator with minimum generation of 100 MW and maximum generation of 200 MW can be dispatched at 0 MW, or anywhere between 100-200 MW;
- The generation sector comprises of :
  - Three baseload generators totalling 1,200 MW, with low marginal cost of production, but high start-up and shut-down costs;
  - Two mid merit plants totally 350 MW, with moderate startup and shutdown costs and higher marginal costs than the baseload units;
  - Six peaking plants, with very low startup and shutdown costs; and
  - One Generator with very flexible production levels, but very high (\$1000/MWh) costs, this is to reflect that the system might run out of capacity for some trading intervals. This can be thought of as approximating a situation where generators offer higher than their marginal costs in the NEM during periods of high demand and limited supply/ Thist has not been fed back to the electricity industry in the CGE model as super-normal profits at this stage.

The model is highly simplified to accommodate fast solution times. For example, no generator ramp-rates or minimum up or down-times are contained in the model at this stage. Including generator ramp rates was trialled but this dramatically increased model run times.

#### Link between Models and the Policy Shock

The integration between the two models assumes that the 335 trading intervals equates to one year in the CGE model. In reality, there are 17,520 trading intervals during a non-leap year.

The electricity model is treated as a cost calculator in the CGE model, rather than as a market in its own right. It effectively calculates the fuel cost (or price of the resource industry commodity) for the CGE electricity industry.

The process is best explained by outlining the policy shock in this paper. The shock is in the form of a 200 MW renewable generator entering the system. It is a short-run simulation, so the model does not consider the investment cost of the new generator. Rather, it just appears in the electricity industry capital stock and is automatically valued at its rental value.

Electricity production for the renewable intermittent generator is simulated with production rising and falling according to a Sine Curve;

- Two scenarios are examined for renewable production. The first has production from the new generator correlating with demand, reducing the system's demand peaks and not affecting offpeak production.
- The second correlates negatively with demand, leaving the system peaks unaffected but the offpeak troughs lower than beforehand; and
- The renewable generator is said to have 'dispatch priority', where it is dispatched whenever the wind is blowing. This is consistent with arrangements in electricity markets around the world<sup>17</sup>.

Demand for the initial fossil-fuel industries after the renewable generator has dispatched under both scenarios is shown in Figure 11 below.



<sup>&</sup>lt;sup>17</sup> Can turn off if price too low.

The renewable generator's marginal cost is zero<sup>18</sup> when it is running, but its production is intermittent depending on the availability of the resource, with no energy storage possible. This might be because the wind does not blow or the sun does not shine all of the time.

The steps to implement this shock into the two models are numerous and outlined below.

- Calculate the original average price of electricity in the electricity industry/commodity by running the electricity market model separately. This is **AP0**.
- Run the CGE model with an increase in capital of 6.3% (200 MW divided by 3,150 MW) in the electricity industry;
- Calculate the change in the quantity of capital in the electricity generation industry and the change in fuel input price (from the resources industry) to the electricity generation industry.
- Loop the two models as follows:

While C\_DIFF>tol\_C or Q\_DIFF>tol\_Q (see below for definitions):

Calculate remaining demand for traditional generators by subtracting renewable production from the original production. This reduction in traditional electricity demand is then increased by the increase in production from the CGE model in **QELEC\_CGE**<sup>1</sup>.

The marginal cost for each generator is increased by the increase in the price of resources industry output used by the electricity industry from the initial CGE run. This is **PRES\_CGE**<sup>1</sup>.

The electricity dispatch model is run with demand and generator costs affected by Z\_CGE and A\_CGE. The model calculates an average price for electricity for the remaining demand. This is then adjusted for the zero marginal cost energy from the renewable source to find **AP** and **dp**=(AP-AP0)/AP0.

The value for dp is fed into the CGE model as an exogenous value for the cost of intermediate inputs purchased by the electricity industry and the CGE model is run again. Updated value for PRES\_CGE<sup>2</sup> and QELEC\_CGE<sup>2</sup> are calculated.

**C\_DIFF** and **Q\_DIFF** are calculated as the difference between the original values for PRES\_CGE and QELEC\_CGE and the updated values.

Specify tolerances for each of C\_DIFF (**tol\_C**) and Q\_DIFF (**tol\_Q**) that are acceptable to the modeller for convergence.

If the either difference is larger than its respective tolerance, the updated values of Z\_CGE and A\_CGE are fed back into the electricity model and so on.

• The adjustment process in this loop is specified as a full adjustment process, where the exogenous inputs are imposed at less than the change from the alternative

<sup>&</sup>lt;sup>18</sup> The vast majority of costs in currently-know renewable technologies are fixed capital costs.

model. For the shock implemented in this paper there is no value recycling where values do not converge, or explosive cycling where the values move away from convergence.

The speed of convergence depends on the power of computer and type of solver involved, but is usually less than 20 seconds for around 3-5 loops for convergence. This compares to Adams et al. (2016), which notes a typical count of three loops before MMRF and WHIRLYGIG results converge.

#### **Results**

The results of the from the stand-alone CGE simulation, the CGE model with positively correlated renewable energy and CGE scenario with negatively correlated renewable energy are shown in Table 1. The levels of various electricity prices from each scenario are also shown.

The simulation has added capital for no investment cost, which is an old consultant's trick to curry favour with governments to support their client's projects, so is expected show some aggregate economic benefit. The initial CGE simulation shows that this is the case.

Table 1: CGE/Electricity Market Model Results from the Addition of a 200 MW Renewab	le
Generator (% Change unless otherwise stated)	

	Original (no electricity model) CGE Results	CGE Results with Electricity Model Positive Correlation	CGE Results with Electricity Model Negative Correlation
Production of Electricity Industry	1.85	02.41	1.60
Aggregate Prices	-0.027	-3.72	1.50
Aggregate Consumption	1.84	5.43	2.00
Price of Electricity	-0.597	-27.70	8.95
Price of Electricity Fuel Input	4.99	-31.80	17.90
Average Marginal Fuel Cost of Fossil Fuel Generation	na	\$56.92/MWh	\$102.34/MWh
Average Marginal Fuel Cost of All Generation	na	\$54.42/MWh	\$97.11/MWh

Note: the original Electricity Price from the initial electricity market simulation (AP0) was \$81/MWh<sup>19</sup>

However, when the electricity model is integrated to the CGE model, several things happen:

- In the stand-alone electricity model, electricity prices fall faster than the CGE model predicts in the for the positive correlation scenario, but rise very slightly in the negative correlation scenario;
  - This is because the additional supply during low demand periods in the negative correlation scenario forces base load generators into costly start-ups and shut-downs and to run more expensive mid-merit generators during offpeak periods<sup>20</sup>;
- In both scenarios, the rise in economic activity in the intial CGE simulation causes the prices of the resources industry, which supplies the electricity industry's main commodity input, to rise;
- This increase in input prices feeds through to increasing electricity prices, which loops through the model back to increasing fuel input prices;
- The final electricity prices in both scenarios are higher than where the stand alone CGE model and stand-alone electricity model originally predicted, although the price in the positive correlation simulation is much lower than the original or base price; and
- The price of electricity in the negative correlation simulation is almost twice that in the positive correlation scenario.

These results, while very preliminary, show that the shape of the renewable production curve relative to the system demand curve is critical to calculating the economic impact of adding such technologies to an electricity system. The currently topical 'duck curve' in California (California Independent System Operator, 2016) shows the difficulty a system might experience if too much electricity is produced at low demand time.

For a model of this type to be truly useful it needs a theory of investment, capital growth and capital retirement in the electricity industry that integrates into both the CGE and electricity models. Additionally, commercially viable electricity storage may be available in the future, which will need to be incorporated into the electricity model.

## Discussion

The examples presented in this paper are specific to the precise models, databases and policy shocks presented. This paper does not examine whether the results are applicable to more general and realistic models and the number areas for development before they could be considered useful models is virtually endless.

Nevertheless, for the specific cases considered, this paper shows that:

<sup>&</sup>lt;sup>19</sup> The prices in the stand-alone electricity market model, with original demand minus renewable supply, were \$49.84/MWh and \$82.74/MWh.

<sup>&</sup>lt;sup>20</sup> This does not include additional ancillary services costs (e.g. additional load following costs) that renewable impose on the system.

- Small-scale comparative-static and recursive-dynamic CGE models can be built in the Python Pyomo package;
- Static expectations may lead to a smaller investment shock than is warranted in response to a known but phased-in policy shock;
- Construction of an integrated CGE model and electricity model is possible; and
- The economic impact of new non-storable renewable energy generation entering the energy sector depends critically on how production from this new industry correlates with electricity demand.

Given the development of substantial development of GEMPACK over many years it is unlikely that the first bullet point is little more than a novelty. Additionally, while not certain, modification of the Dixon et al. (2003) algorithm to look forward past year t+1 would probably be able to be accommodated with GEMPACK and its associated dynamic modelling software.

Undertaking an integrated CGE and electricity model would be a substantial undertaking and no claim is made regarding whether this is a worthwhile exercise. However, exact specification of the stationary energy sector is important to policy questions that are likely to become more important over the next decade. It is not clear whether this could be accommodated directly into GEMPACK.

Practical implementation of the concepts examined in this paper would require substantial computing power. However, computing power continues to improve enormously. For example, computers are much more powerful in 2016 than then when Dixon el al. (2003) noted that solving a fully dynamic model was computationally intensive.<sup>21</sup>

Additionally, the pioneering CGE modellers in Australia were not deterred by daunting computing tasks. The original ORANI model was run on the external CSIRO's CYBER 76 computing system, with charges of \$50 (in 1977 prices) to run the model (Sutton, 1977). In the early 1980s ORANI was still solved on the CSIRO mainframe computer where modellers would submit data cards and wait overnight for the model to run (Horridge, Meeraus, Pearson and Rutherford, 2013). They did so, presumably, because they thought the results were vital enough to wait for. The question is still whether the results are worth the wait.

<sup>&</sup>lt;sup>21</sup> The difficulty of interpreting non-linear equations still remains.

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CC	GE and DSGE: strengths and weaknesses
CGE strength	- structural detail
CGE weakness	- rudimentary macro, backward-looking expectations, decision making under certainty
DSGE strength	- agents at year t form forward-looking expectations taking account of the current situation and their estimates of probability distributions for future variables
DSGE weakness	- rudimentary structural detail
Aim:	Create an integrated CGE/DSGE model for Australia to be run in GEMPACK Make GEMPACK a user friendly platform for DSGE modelling
2	









Since  $J(X_t,\sigma) = 0$  for all values of  $X_t$  and  $\sigma$ , the derivatives of any order of J with respect to  $X_t$  and  $\sigma$  must be zero

This allows us to evaluate derivatives of the policy function G without knowing the levels form of G.

For GEMPACK users this is a familiar idea. We have a model of the form  $M(V_1,V_2)=0 \label{eq:model}$ 

where V<sub>1</sub> and V<sub>2</sub> are vectors of endogenous and exogenous variables.

We would like to express  $V_1$  as a function of  $V_2$ :  $V_1 = N(V_2)$ We know the form of M but it is impossible to find an explicit form of N. However, we can evaluate derivatives of the unknown function N by totally differentiating M, leading to the familiar

$$\mathbf{v}_1 = -\mathbf{A}_1^{-1} * \mathbf{A}_2 * \mathbf{v}_2$$

7

where  $A_1$  and  $A_2$  are matrices of first-order derivatives of M evaluated at an initial solution,  $-A_1^{-1} * A_2$  is the matrix of first order derivatives (or elasticitites) of N with respect to  $V_2$  and  $v_1$  and  $v_2$  are percentage deviations of  $V_1$  and  $V_2$  away from the initial solution

 $\mathbf{Y}_{t+1} \qquad \mathbf{Y}_{t} \qquad \mathbf{X}_{t+1} \qquad \mathbf{X}_{t}$  $\mathbf{J}^{i}(\mathbf{X}_{t},\sigma) = \mathbf{E}_{t} \Big[ \mathbf{F}^{i} \Big( \mathbf{G}(\mathbf{e}^{\sigma \mathbf{Z} \mathbf{s}_{t+1}} * \mathbf{H}(\mathbf{X}_{t},\sigma),\sigma) ; \mathbf{G}(\mathbf{X}_{t},\sigma) ; \mathbf{e}^{\sigma \mathbf{Z} \mathbf{s}_{t+1}} * \mathbf{H}(\mathbf{X}_{t},\sigma) ; \mathbf{X}_{t} \Big) \Big] = 0$  $\mathbf{i} = 1, 2, ..., \mathbf{n}_{y}$  $\left( \mathbf{J}_{\mathbf{X}}^{i} \right)_{\mathbf{m}} = 0, \quad \mathbf{m} = 1, 2, ..., \mathbf{n}_{x} \qquad (7)$  $\left( \mathbf{J}_{\mathbf{X}}^{i} \right)_{\mathbf{m}} = \mathbf{E} \Big[ \sum_{\alpha, \beta} \Big( \mathbf{F}_{y_{1}}^{i} \Big)_{\alpha} \Big( \mathbf{G}_{x_{1}}^{\alpha} \Big)_{\beta} * \mathbf{e}^{\sigma \mathbf{Z}^{\beta_{g}}} * \Big( \mathbf{H}_{x}^{\beta} \Big)_{\mathbf{m}} + ... + \Big( \mathbf{F}_{x}^{i} \Big)_{\mathbf{m}} \Big] = 0$ 



#### CoPS How to solve for $\bar{\mathbf{G}}_{\mathbf{x}}$ in GEMPACK Obtain steady-state solution, $\bar{X}, \bar{Y}$ Evaluate derivatives of F and $\hbar$ at the steady-state solution. GEMPACK can do this for us. Write linearized form of (18): $(d\overline{G}_x) = d_{slack}$ Conduct simulation in which d\_slack moves exogenously to zero. Equation E\_d\_slack $(All,i,NY)(All,m,NX) d\_slack(i,m) = - SLACK\_B(i,m)*del\_unity;$ Equation E\_d\_g\_x (All,i,NY)(All,m,NX) d\_SLACK(i,m) = $Sum(j,NY, Sum(k,NX, F_Y1(i,j)*[H_X(k,m)*d_G_X(j,k) + Sum(l,NY, H_Y(k,l)*G_X(j,k)*d_G_X(l,m))) = (1 + 1) + (1 + 1)$ $+Sum(1,NY, H_Y(k,1)*G_X(1,m)*d_G_X(j,k))]))$ + **Sum** $(j,NY, F_Y(i,j)*d_G_X(j,m))$ + $Sum(j,NX, F_X1(i,j)*[+Sum(l,NY, H_Y(j,l)*d_G_X(l,m))])$ 11



# Introducing the policy rule to GEMPACK

**Policy rule:**  $Y_t = G(X_t)$ 

Second-order Taylor approximation

$$\mathbf{Y}_{t} = \overline{\mathbf{Y}} + \left(\overline{\mathbf{G}}_{x}\right)^{*} (\mathbf{X}_{t} - \overline{\mathbf{X}}) + \frac{1}{2}^{*} (\mathbf{X}_{t} - \overline{\mathbf{X}})^{*} \overline{\mathbf{G}}_{xx}^{*} (\mathbf{X}_{t} - \overline{\mathbf{X}}) + \frac{1}{2}^{*} \sigma^{*} \overline{\mathbf{G}}_{\sigma\sigma}^{*} \sigma \quad (22)$$

**Representation in GEMPACK** 

$$\mathbf{d}_{\mathbf{Y}} = \left(\overline{\mathbf{G}}_{\mathbf{x}}\right)^* (\mathbf{d}_{\mathbf{X}}) + (\mathbf{X} - \overline{\mathbf{X}})'^* \overline{\mathbf{G}}_{\mathbf{xx}}^* (\mathbf{d}_{\mathbf{X}}) + \sigma^* \overline{\mathbf{G}}_{\sigma\sigma}^* \mathbf{d}_{-\sigma}$$
(23)

13

#### Solving a 1-sector DSGE model in GEMPACK

$$\begin{split} \mathbf{K}_{\tau+1} &- \mathbf{K}_{\tau} (1-\delta) - \mathbf{K}_{\tau}^{\alpha} \mathbf{A}_{\tau} + \mathbf{C}_{\tau} = 0, \qquad \tau = t, t+1, \dots, \infty \quad (\mathbf{B2}) \\ \mathbf{A}_{\tau+1} &= e^{\sigma \mathbf{e}_{\tau+1}} * \mathbf{A}_{0} \qquad \tau = t, t+1, \dots, \infty \quad (\mathbf{B3}) \\ \mathbf{E}_{\tau} \Big[ \beta \mathbf{C}_{\tau+1}^{-\gamma} \Big( (1-\delta) + \alpha \mathbf{K}_{\tau+1}^{\alpha-1} \mathbf{A}_{\tau+1} \Big) - \mathbf{C}_{\tau}^{-\gamma} \Big] = 0, \quad \tau = t, t+1, \dots, \infty \quad (\mathbf{B4}) \end{split}$$

Parameter values:  $\delta = 0.08$ ;  $\gamma = 0.999$ ;  $\beta = 0.96$ ;  $\alpha = 0.36$ ;  $A_0 = 1$ Set  $\sigma = 0$ , find  $(\overline{C}, \overline{A}, \overline{K})$  $\overline{A} = A_0 = 1$  $\beta \overline{C}^{-\gamma} ((1-\delta) + \alpha \overline{K}^{\alpha-1} \overline{A}) - \overline{C}^{-\gamma} = 0$  implies  $\overline{K} = 5.447$ 

 $\overline{\mathbf{K}} - \overline{\mathbf{K}} (1 - \delta) - \overline{\mathbf{K}}^{\alpha} \overline{\mathbf{A}} + \overline{\mathbf{C}} = 0$  implies  $\overline{\mathbf{C}} = 1.405$ 





## Immigration reform scenarios for U.S. agriculture

CoPS

by Peter B. Dixon and Maureen T. Rimmer Centre of Policy Studies, Victoria University

Presentation by Maureen T. Rimmer National CGE Conference Canberra August 8, 2016



## Previous work on immigration



Our previous studies for the U.S. Departments of Homeland Security, Commerce and Agriculture and the Cato Institute have dealt with general policies of tighter border security, control of employers, legalization and guest worker programs. See:

Dixon, P.B. and Maureen T. Rimmer (2009), "Restriction or Legalization? Measuring the economic benefits of immigration reform", Trade Policy Analysis paper no. 40, Cato Institute, Washington DC, August, pp. 22.

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## Exposition via a Minimal model

In this presentation we convey the essential features of USAGE and its results on immigration policies for agriculture by building and applying a model that embraces the minimal ingredients necessary to explain the effects of supplementing supply of labour to agriculture via foreign workers.

The Minimal model has:

- 2 sectors (agriculture/non-agriculture)
- labour supply consisting of: a fixed number of incumbent hired workers who can move between agriculture and non-agriculture in response to changes in relative wage rates; a fixed number of farmers who work in agriculture only; and an exogenous quantity of foreign labour assigned to agriculture
- · measures of welfare for farmers and more generally for incumbents

For expositional purposes, an advantage of the Minimal model is that the variables, coefficients, parameters and equations can be listed in relatively small tables.

We set up the database for the Minimal model so that the cost-structure and relative size of the agricultural sector is realistic

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### Database for Minimal Model: Values of flows in base year

	Industry 1 (ag)	Industry 2 (non-ag)	Consumption
Commodity 1 (ag)	0	0	2.00
Commodity 2 (non-ag)	0	0	98.00
Competitive farmer labour	0.53	0	
Hired incumbent labour	0.28	93.10	
Foreign labour	0.19	0	
Fixed factor	1.00	4.90	
Cost (output)	2.00	98.00	

#### Percentage effects of a 50% increase in the supply of foreign labour to agriculture: results from the Minimal model

	Simulation:	1	2	3	- 4
	Elasticity of substitution	1.000	1.000	1.1725	1.000
	in consumption, $\sigma_c$				
	Farmer competitive labour	1	1	1	0.81
	share				
	Initial Ag/NonAg wage	0.5	1	0.5	0.5
	ratio				
	Results:				
1	GDP	0.137	0.093	0.136	0.140
2	Aggregate employment,				
	wagebill weights	0.146	0.099	0.145	0.149
3	Aggregate employment,				
	persons	0.200	0.101	0.200	0.200
4	Employment, Agric	5.078	5.058	5.169	5.274
5	Employment, Non-Agric	0.095	0.048	0.093	0.102
6	Incumbent welfare	0.066	0.021	0.064	0.071
7	Direct effect	0.020	0.020	0.019	0.021
8	Occupation-mix effect	0.044	0.000	0.043	0.048
9	Farm income	-0.336	-0.379	0.000	0.087
10	Agricultural output	2.462	2.452	2.505	2.291
11	Agricultural prices	-2.269	-2.304	-1.975	-2.103
12	Real wages, Agric	-8.248	-8.258	-8.075	-8.901
13	Real wages, NonAgric	0.035	0.042	0.029	0.031

#### Percentage effects of a 50% increase in the supply of foreign labour to agriculture: results from the Minimal model

	Simulation:	1	2	3	- 4
	Elasticity of substitution	1.000	1.000	1.1725	1.000
	in consumption, $\sigma_c$				
	Farmer competitive labour	1	1	1	0.81
	share				
	Initial Ag/NonAg wage	0.5	1	0.5	0.5
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10	Agricultural output	2.462	2.452	2.505	2.291
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12	Real wages, Agric	-8.248	-8.258	-8.075	-8.901
13	Real wages, NonAgric	0.035	0.042	0.029	0.031

			•		
	Circuitedian				
	Simulation:	1 000	1.000		4
	Elasticity of substitution	1.000	1.000		
	In consumption, $\sigma_c$	1	1		
	share	1	1		
	Initial Ag/NonAg wage	0.5	1		
	ratio				
	Results:				
1	GDP	0.137	0.093	0.136	0.140
2	Aggregate employment,				
	wagebill weights	0.146	0.099		
3	Aggregate employment,				
	persons	0.200	0.101		
4	Employment, Agric	5.078	5.058		
5	Employment, Non-Agric	0.095	0.048		
6	Incumbent welfare	0.066	0.021		
7	Direct effect	0.020	0.020		
8	Occupation-mix effect	0.044	0.000		
9 10	Farm income	-0.336	-0.379		
10	Agricultural prices	2.462	2.452		
12	Agricultural prices	-2.269	-2.304		
13	Real wages, Agric	-0.240	-0.230		
15	Real wages, RollAgrie	0.055	0.042	0.022	0.051











Simulation:	1	2	3	4
Elasticity of substitution	1.000		1.1725	1.000
in consumption, σ <sub>c</sub>				
Farmer competitive labour	1	1	1	
share				
Initial Ag/NonAg wage	0.5	1	0.5	
ratio	<u>_</u>	<u> </u>	<u>_</u>	
Results:				
GDP	0.137	0.093	0.136	0.140
Aggregate employment,				
wagebill weights	0.146		0.145	0.149
Aggregate employment,				
persons	0.200		0.200	
Employment, Agric	5.078	5.058	5.169	5.274
Incumbent welfere	0.095	0.048	0.093	0.102
Direct offect	0.000	0.021	0.004	0.071
Occupation-mix affect	0.020		0.019	
Farm income	-0.336	-0.379	0.000	0.087
Agricultural output	2.462	2.452	2.505	2.291
Agricultural prices	-2.269	-2.304	-1.975	-2.103
Real wages, Agric	-8.248	-8.258	-8.075	-8.901
Real wages, NonAgric	0.035	0.042	0.029	0.031

#### Percentage effects of a 50% increase in the supply of foreign labour to agriculture: column 4, lower share of farmer labour competes with hired labour

	Simulation:	1	2	3	4
	Elasticity of substitution	1.000			1.000
	in consumption, $\sigma_c$				
	Farmer competitive labour	1			0.81
	share				
	Initial Ag/NonAg wage	0.5			0.5
	ratio				
	Results:				
1	GDP	0.137	0.093	0.136	0.140
2	Aggregate employment,				
	wagebill weights	0.146			0.149
3	Aggregate employment,				
	persons	0.200			0.200
4	Employment, Agric	5.078			5.274
5	Employment, Non-Agric	0.095			0.102
6	Incumbent welfare	0.066			0.071
7	Direct effect	0.020			0.021
8	Occupation-mix effect	0.044			0.048
9	Farm income	-0.336			0.087
10	Agricultural output	2.462			2.291
11	Agricultural prices	-2.269			-2.103
12	Real wages, Agric	-8.248			-8.901
13	Real wages, NonAgric	0.035			0.031

## **Concluding Remarks** Policy makers want realistic detail. Consequently we build large detailed models.

CoPS

These models often reveal policy-relevant insights that we wouldn't have thought of *a priori*, e.g. the occupation-mix effect and the potential negative relationship between immigration policies designed to support agriculture and farm income.

Academics display little patience in understanding detailed models and are sceptical of their results.

How can we bring big model insights to the attention of academics?

We are trying to do so through construction of Minimal easily absorbed models.

We should emphasize however that the big model comes first. Results from the big model suggest what must be encapsulated in the Minimal model.



























9

# Modelling demographic change and economic growth

Dynamic model of global economics and demographics to 2050

- 18 regions, of which China is one
- 16 households in each region are age-gender-skill groups with populations driven by endogenous births, deaths, survival and migration flows
- Labour force participation is modelled explicitly so that dependency ratios are based on <u>employed</u> populations
- Industries: agriculture, light manufacturing, heavy manufacturing, energy, metals, minerals, services
- · Factors: skilled labour, unskilled labour, capital, land, natural resources
- · Endogenous growth: capital accumulation, demographic change, skill upgrading
- · Exogenous growth: technical change by factor and industry, common to all scenarios
- · Open capital accounts with investment abroad via a global trust
- Consumption & saving group-specific, responsive to real per capita disposable income and real private rates of return on saving

Real exchange rates driven by differentiated products and little-traded services

## Simulations to 2050

#### Baseline

'High GDP growth' scenario

The 2CP is successful, moving fertility to sustainable population Saving rates decline only moderately with ageing

#### Low saving only

'Dual policy success' scenario

The 2CP is successful, moving fertility to sustainable population

The rebalancing push sees saving rates decline to advanced region levels by 2050

#### Low fertility only

Fertility continues to decline, roughly in the manner of the UN low growth case Saving rates decline only moderately with ageing

#### Low saving and low fertility

'Double contraction' scenario

Fertility continues to decline, roughly in the manner of the UN low growth case

The rebalancing push sees saving rates decline to advanced region levels by 2050




















































# Change in real per capita income

(%	rela	tive	to	base	line)	)
----	------	------	----	------	-------	---

	Low fertility,	High fertility, low	Low fertility,
	high saving	saving	low saving
Australia	-0.1	-2.9	-3.0
USA	-0.3	-1.1	-1.4
Canada	-1.5	-3.5	-4.8
Mexico	-0.8	-6.2	-6.9
Western Europe	-0.9	-1.4	-2.2
Russia and Eastern Europe	-3.2	-5.2	-8.3
Japan	-1.0	0.8	-0.4
China	20.7	-15.4	-2.7
Taiwan	-0.7	-1.0	-1.8
Hong Kong	-1.3	-1.4	-2.6
Indonesia	-0.1	-2.9	-2.8
Other East Asia	-0.6	-3.6	-4.0
India	4.6	-0.3	3.9
Other South Asia	0.8	-1.6	-0.8
Latin America	-1.5	-4.7	-5.9
ME and Nth Africa	-1.7	-4.7	-6.1
Sub-Saharan Africa	-0.9	-2.7	-3.3
Rest of world	-1.6	-3.2	-4.7

Bottom line: Chinese growth slowdown hits everywhere but India. But good news is that impacts not huge for Australia

But good news is that impacts not nuge for Austral

## MODELLING THE POTENTIAL IMPACTS OF ECONOMIC REFORM IN A PARTNERSHIP BETWEEN AUSTRALIA AND CHINA

Paul Gretton East Asian Bureau of Economic Research, ANU

Presentation to: National CGE Workshop Old Parliament House, Canberra, 8 August 2016

## Context and scenarios modelled

- Joint study of the economic relationship between Australia and China
  - by East Asian Bureau of Economic Research (EABER), ANU; China Center for International Economic Exchanges (CCIEE), Bejing.
- The effects of an economic reform program are specific to the reform modalities, the barriers to efficiency, economic structure
- GTAP model used to project the implications for Australia & China of
  - Preferential, unilateral and broader approaches to trade liberalisation
  - A broad agenda for productivity improving reform across services
  - Financial market reform

## Modelling approach

- GTAP variant that used by PC (2010) study on trade agreements
- Database
  - 20 national economies Australia and China separate
  - plus, 5 multi-country regions
  - 57 industry groups 14 Agriculture etc; 4 Mining; 24 Manufacturing; 15 Services
- Comparative-static compares the global economy with and without the changes applied, allowing for full adjustment
- Longer term regional industry rates of return fixed; industry capital stocks adjust
- Aggregate labour supply unchanged by policies, labour mobile between regional industries
- DB for 2004 year, abstracts from GFC and ToT boom, but misses longer-term changes

## Reduction in border assistance

- The border protection represented by the tariff revenue associated with the protection measure (not power of tariff)
- Tariff revenue recorded on bilateral basis enables simulation of preferential, unilateral and multilateral scenarios
  - Key assumption all 'tariff assistance' is measured in the tariff revenue variable: tms (i, r, s)
- Some mfn tariff reductions since 2004 broad policy message robust

# Gains from bilateral reductions modest, unilateral liberalisation likely to dominate

	Simulation	Australia Share of world	China Share of world	
		%	%	
T1	Australia-China bilateral	23	4	
Т2	Australia unilateral	60	1	
Т3	China unilateral	13	78	
Т4	RCEP open regionalism	94	81	
тс	World MFN liberalization	100	100	
15	Projected change in GDP	0.94	2.94	



# With differing industry structures, impact differs between Australia and China

			GDP gain	GDP gain
_		Simulation	Australia	China
			% change	% change
	S1	Australian services	1.13	
	S2	Chinese services	0.01	0.68

• As China transitions toward a more open and services oriented economy, the dividend could rise commensurately

Sectoral impacts vary [qva (prodcomm, reg)]

	Primary	Manufacturing	Services
Australia	+	+	+
China	+	+	-

# Financial market reform can help facilitate the flow of savings to the most productively efficient investments, improve access to capital & reduce the risk premium on capital finance Basic concept: $r_t^i = r_t^U + e_t^i + \varepsilon_t^i$ , where r is the real rate of interest in period t in region r $r_t^U$ is the real rate of interest in a reference economy – the US $e_t^i$ is the error in expectation of the real exchange rate $\varepsilon_t^i$ is a measure of factors including sovereign risk, impediments to financial flows and other factors affecting real interest rates differentials Shift term in the relation rorc\_(r,s) = rorc\_s(r) + f\_rorc\_(r,s) targeted – new to PC variant $\rightarrow \downarrow pK$ (r,s) – the rental price of capital

# Some information available on ror wedges between China and US

	G-Cubed	GTAP model dat	ta base
	1996	2004	2011
	%	%	%
China	4.15	5.08	2.12

- Modelled elimination of ½ of the wedge in 2011 ie, a permanent 106 basis point (1.06 percentage point) reduction
- Lower end of possible range?

Australia		China			
GDP	GNP	GDP	GNP		
% change	% change	% change	% change		
0.06	0.06	5.72	5.51		
ome regio	nal realloc	ation of ac	tivity project	ed	
onne regio					
	Compet	titors (eg			
Suppliers to	Compet o Korea, 1	titors (eg Fhailand,			

## Conclusion and further research

- Significant economic gains are available from trade liberalising, service industry productivity and financial market reforms
  - Bilateral preferential liberalisation is least advantageous strategy
- Opportunities for further research
  - links between individual reform proposals and potential economic gains
  - the distributional effects of potential impacts industry, region, households
  - the time horizon over which reforms may be implemented and take effect a dynamic approach ...
  - ... effects of changing industry , trade and institutional environment in China, Australia and other trading partners



### Solving a partial equilibrium model in a CGE framework: the case of a BMS model

Xiao-guang Zhang Productivity Commission, Australia

National CGE Workshop, August 8, 2016, Canberra















Productivity Commission











































# Economic benefits from Fisheries reforms

How CGE modelling should influence policy advice

# Context – how much should Govt be willing to spend on reform?

- We can work through the problem logically using a CGE model to shed light on the issue in question
- Government should be willing to spend an amount up to the economic benefits reforms might bring, taking into account the likelihood that the reform actions would work, and less the deadweight loss from taxation
- The East Coast Trawl Fishery as an example

2 TITLE OF PRESENTATION GOES IN FOOTER www.synergies.com.au

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	2018	2019	2020	2021	2022	2023	2024	2025	2026
Economic rent	9.5	17.9	24.9	31.8	38.5	35.3	33.1	31.9	30.8
louseholds	4.7	9.2	13.4	17.7	22.1	21.8	21.9	22.2	22.4
Government	0.9	1.7	2.5	3.3	4.1	4.1	4.1	4.2	4.3
Households Government Leakages →	4.7 0.9 foreigne	9.2 1.7 ers and	13.4 2.5	17.7 <u>3.3</u>	22.1 4.1	21.8 4.1	21.9 4.1	22.2 4.2	2

н	ow the benefits co	ompare		
	Reform	Benefits		
	Trading hour restrictions	\$200 million pa		
	Taxi license restrictions	\$6 – 20 million pa		
	Queensland gas scheme	\$12 – 53 million pa		
	East Coast Trawl reforms	\$25 + million pa		
	Source: CIE, prioritisation of regulatory reforms, 2012.			
18 TITLE OF F www.synergie	RESENTATION GOES IN FOOTER	c Consulting 2013	Syn	ergies



















Alternative scenarios
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Main (M)	SIGMA_LK = 0.4
High SIGMA (HS)	SIGMA_LK = 0.8
Funded (RN)	TAXREV/GDP fixed, tax on wages increases
Early investment (EI)	Foreign investment starts responding before tax cut
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